

SET ~ 3

प्रश्न-पत्र कोड
Q.P. Code **30/4/3**

परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।
Candidates must write the Q.P. Code on the title page of the answer-book.

NOTE

- (I) Please check that this question paper contains **15** printed pages.
- (II) Please check that this question paper contains **38** questions.
- (III) Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
- (IV) **Please write down the Serial Number of the question in the answer-book at the given place before attempting it.**
- (V) 15 minutes time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the students will read the question paper only and will not write any answer on the answer-book during this period.

MATHEMATICS (STANDARD)

Time allowed : 3 hours

Maximum Marks : 80

General Instructions :

Read the following instructions carefully and follow them :

- (i) This question paper contains **38** questions. **All** questions are **compulsory**.
- (ii) This question paper is divided into **five** Sections – **A, B, C, D** and **E**.
- (iii) In **Section A** – Question numbers **1** to **18** are multiple choice questions (MCQs) and question numbers **19** and **20** are Assertion – Reason based questions of **1** mark each.
- (iv) In **Section B** – Question numbers **21** to **25** are very short answer (VSA) type questions, carrying **2** marks each.
- (v) In **Section C** – Question numbers **26** to **31** are short answer (SA) type questions, carrying **3** marks each.
- (vi) In **Section D** – Question numbers **32** to **35** are long answer (LA) type questions carrying **5** marks each.
- (vii) In **Section E** – Question numbers **36** to **38** are **case-study based integrated** questions carrying **4** marks each. Internal choice is provided in **2** marks question in each case-study.
- (viii) There is no overall choice. However, an internal choice has been provided in **2** questions in Section **B**, **2** questions in Section **C**, **2** questions in Section **D** and **3** questions of **2** marks in Section **E**.
- (ix) Draw neat diagrams wherever required. Take $\pi = \frac{22}{7}$ wherever required, if not stated.
- (x) Use of calculators is **NOT** allowed.

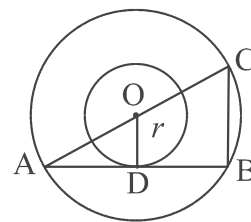
SECTION – A

20×1 = 20

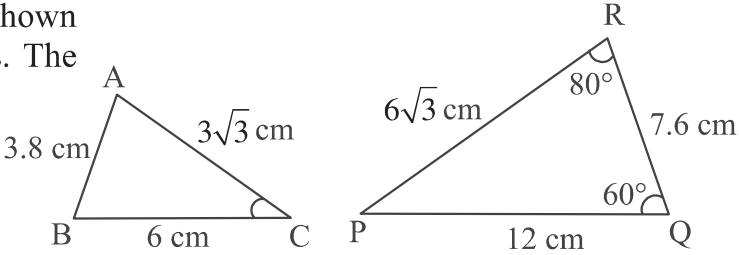
This section consists of 20 questions of 1 mark each.

- 1. A 30 m long rope is tightly stretched and tied from the top of pole to the ground. If the rope makes an angle of 60° with the ground, the height of the pole is : **1**
(a) $10\sqrt{3}$ m (b) $30\sqrt{3}$ m (c) 15 m (d) $15\sqrt{3}$ m
- 2. On the top face of the wooden cube of side 7 cm, hemispherical depressions of radius 0.35 cm are to be formed by taking out the wood. The maximum number of depressions that can be formed is : **1**
(a) 400 (b) 100 (c) 20 (d) 10
- 3. The cumulative frequency for calculating median is obtained by adding the frequencies of all the : **1**
(a) classes up to the median class
(b) classes following the median class
(c) classes preceding the median class
(d) all classes
- 4. If mode and median of given set of observations are 13 and 11 respectively, then the value of mean is : **1**
(a) 17 (b) 7 (c) 10 (d) 28

5. In the adjoining figure, AC is diameter of larger circle with centre O. AB is tangent to smaller circle with centre O. If $OD = r$, then BC is equal to :



- (a) r (b) $\frac{3r}{2}$
 (c) $2r$ (d) $4r$ 1
6. A parallelogram having one of its sides 5 cm circumscribes a circle. The perimeter of parallelogram is : 1
 (a) 20 cm (b) less than 20 cm
 (c) more than 20 cm but less than 40 cm (d) 40 cm
7. E and F are points on the sides AB and AC respectively of a ΔABC such that $\frac{AE}{EB} = \frac{AF}{FC} = \frac{1}{2}$. Which of the following relation is true ? 1
 (a) $EF = 2BC$ (b) $BC = 2EF$ (c) $EF = 3BC$ (d) $BC = 3EF$
8. Which of the following statements is true for a polynomial $p(x)$ of degree 3? 1
 (a) $p(x)$ has at most two distinct zeroes.
 (b) $p(x)$ has at least two distinct zeroes.
 (c) $p(x)$ has exactly three distinct zeroes.
 (d) $p(x)$ has at most three distinct zeroes.
9. Letters A to F are mentioned on six faces of a die such that each face has a different letter. Two such dice are thrown simultaneously. The probability that vowels turn up on both the dice is : 1
 (a) $\frac{1}{4}$ (b) $\frac{1}{3}$ (c) $\frac{1}{9}$ (d) $\frac{1}{36}$
10. If $x = ab^3$ and $y = a^3b$, where a and b are prime numbers, then $[HCF(x, y) - LCM(x, y)]$ is equal to : 1
 (a) $1 - a^3b^3$ (b) $ab(1 - ab)$
 (c) $ab - a^4b^4$ (d) $ab(1 - ab)(1 + ab)$
11. $(1 + \sqrt{3})^2 - (1 - \sqrt{3})^2$ is : 1
 (a) a positive rational number. (b) a negative integer.
 (c) a positive irrational number. (d) a negative irrational number.
12. The value of 'a' for which $ax^2 + x + a = 0$ has equal and positive roots is : 1
 (a) 2 (b) -2 (c) $\frac{1}{2}$ (d) $-\frac{1}{2}$
13. The distance of point P(1, -1) from x-axis is : 1
 (a) 1 (b) -1 (c) 0 (d) $\sqrt{2}$

14. The number of red balls in a bag is 10 more than the number of black balls. If the probability of drawing a red ball at random from this bag is $\frac{3}{5}$, then the total number of balls in the bag is : 1
 (a) 50 (b) 60 (c) 80 (d) 40
15. The value of ' p ' for which the equations $px + 3y = p - 3$, $12x + py = p$ has infinitely many solutions is : 1
 (a) -6 only (b) 6 only
 (c) ± 6 (d) Any real number except ± 6
16. $\triangle ABC$ and $\triangle PQR$ are shown in the adjoining figures. The measure of $\angle C$ is : 1
 (a) 140°
 (b) 80°
 (c) 60°
 (d) 40°
- 
17. $\sec A = 2 \cos A$ is true for $A =$ 1
 (a) 0° (b) 30° (c) 45° (d) 60°
18. Which of the following statements is true ? 1
 (a) $\sin 20^\circ > \sin 70^\circ$ (b) $\sin 20^\circ > \cos 20^\circ$
 (c) $\cos 20^\circ > \cos 70^\circ$ (d) $\tan 20^\circ > \tan 70^\circ$

Directions :

In question number 19 and 20, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct option :

- (a) Both, Assertion (A) and Reason (R) are true and Reason (R) is correct explanation of Assertion (A).
 (b) Both, Assertion (A) and Reason (R) are true but Reason (R) is not the correct explanation of Assertion (A).
 (c) Assertion (A) is true but Reason (R) is false.
 (d) Assertion (A) is false but Reason (R) is true.
19. **Assertion (A) :** Tangents drawn at the end points of a diameter of a circle are always parallel to each other.
Reason (R) : The lengths of tangents drawn to a circle from a point outside the circle are always equal. 1
20. **Assertion (A) :** Unit digit of 3^n cannot be an even number for any natural number n .
Reason (R) : 2 is not a prime factor of 3^n for any natural number n . 1

SECTION – B

This section consists of 5 questions of 2 marks each.

21. (A) A 1.5 m tall boy is walking away from the base of a lamp post which is 12 m high, at the speed of 2.5 m/sec. Find the length of his shadow after 3 seconds. 2

OR

- (B) In parallelogram ABCD, side AD is produced to a point E and BE intersects CD at F. Prove that $\triangle ABE \sim \triangle CFB$ 2
22. Find the coordinates of the point C which lies on the line AB produced such that $AC = 2BC$, where coordinates of points A and B are $(-1, 7)$ and $(4, -3)$ respectively. 2
23. (A) Find the value of x for which $(\sin A + \operatorname{cosec} A)^2 + (\cos A + \sec A)^2 = x + \tan^2 A + \cot^2 A$ 2

OR

- (B) Evaluate the following : 2
- $$\frac{3 \sin 30^\circ - 4 \sin^3 30^\circ}{2 \sin^2 50^\circ + 2 \cos^2 50^\circ}$$
24. Renu and Simran were born in the year 2000 which is a leap year. Find the probability that : 2
- (i) both have same birthday.
- (ii) both have different birthdays.
25. Solve the following system of equations algebraically : 2
- $$73x - 37y = 109$$
- $$37x - 73y = 1$$

SECTION – C

This section consists of 6 questions of 3 marks each.

26. P (x, y) , Q $(-2, -3)$ and R $(2, 3)$ are the vertices of a right triangle PQR right angled at P. Find the relationship between x and y . Hence, find all possible values of x for which $y = 2$. 3
27. (A) Prove that $\frac{\cos A + \sin A - 1}{\cos A - \sin A + 1} = \operatorname{cosec} A - \cot A$ 3

OR

- (B) If $\cot \theta + \cos \theta = p$ and $\cot \theta - \cos \theta = q$,
prove that $p^2 - q^2 = 4\sqrt{pq}$ 3
28. If α and β are the zeroes of the polynomial $ax^2 - x + c$. Obtain a polynomial whose zeroes are $\alpha - 3$ and $\beta - 3$. 3
29. Rectangle ABCD circumscribes the circle of radius 10 cm. Prove that ABCD is a square. Hence, find the perimeter of ABCD. 3

30. (A) Prove that $\sqrt{2}$ is an irrational number. 3

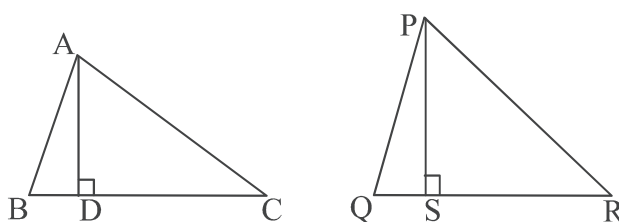
OR

- (B) Let x and y be two distinct prime numbers and $p = x^2 y^3$, $q = xy^4$, $r = x^5 y^2$. Find the HCF and LCM of p , q and r . Further check if $\text{HCF}(p, q, r) \times \text{LCM}(p, q, r) = p \times q \times r$ or not. 3
31. The perimeter of a rectangle is 70 cm. The length of the rectangle is 5 cm more than twice its breadth. Express the given situation as a system of linear equations in two variables and hence solve it. 3

SECTION – D

This section consists of 4 questions of 5 marks each.

32. (A) The corresponding sides of $\triangle ABC$ and $\triangle PQR$ are in the ratio 3 : 5. $AD \perp BC$ and $PS \perp QR$ as shown in the following figures : 5



- (i) Prove that $\triangle ADC \sim \triangle PSR$
- (ii) If $AD = 4$ cm, find the length of PS .
- (iii) Using (ii) find $\text{ar}(\triangle ABC) : \text{ar}(\triangle PQR)$

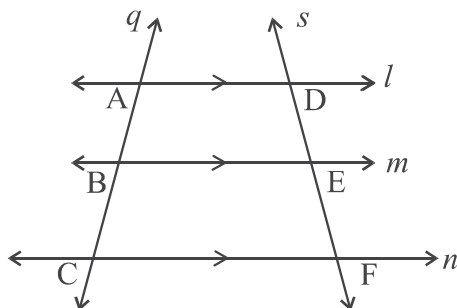
OR

- (B) State basic proportionality theorem.

Use it to prove the following :

If three parallel lines l , m , n are intersected by transversals q and s as shown in the adjoining figure,

$$\text{then } \frac{AB}{BC} = \frac{DE}{EF}.$$



33. A bat manufacturing company made a huge bat for charity and got it signed by world cup winning team. 5

The dimensions of the bat which is in the form of a cuboid with a cylindrical handle at the top are as follows :

length = 2 m, width = 0.5 m, thickness = 0.1 m

diameter of cylindrical part = 0.1 m

height of cylindrical part = 0.7 m

Find the volume of wood used in the bat. Also, find the total surface area of the wooden bat.

34. Following table shows the absentees record of 40 students in an academic year :

Number of Days	Number of Students
2-6	11
6-10	10
10-14	7
14-18	4
18-22	4
22-26	3
26-30	1

Find the 'mean' and the 'mode' of the above data.

5

35. (A) The sides of a right triangle are such that the longest side is 4 m more than the shortest side and the third side is 2 m less than the longest side. Find the length of each side of the triangle. Also, find the difference between the numerical values of the area and the perimeter of the given triangle.

5

OR

- (B) Express the equation $\frac{x-2}{x-3} + \frac{x-4}{x-5} = \frac{10}{3}$; ($x \neq 3, 5$) as a quadratic equation in standard form. Hence, find the roots of the equation so formed.

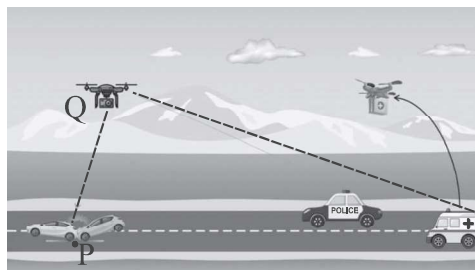
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SECTION – E

This section consists of 3 Case-study based questions of 4 marks each.

36. A drone was used to facilitate movement of an ambulance on the straight highway to a point P on the ground where there was an accident.

The ambulance was travelling at the speed of 60 km/h. The drone stopped at a point Q, 100 m vertically above the point P. The angle of depression of the ambulance was found to be 30° at a particular instant.



Based on above information, answer the following questions :

- Represent the above situation with the help of a diagram.
- Find the distance between the ambulance and the site of accident (P) at the particular instant. (Use $\sqrt{3} = 1.73$)
- (a) Find the time (in seconds) in which the angle of depression changes from 30° to 45° .

1

1

2

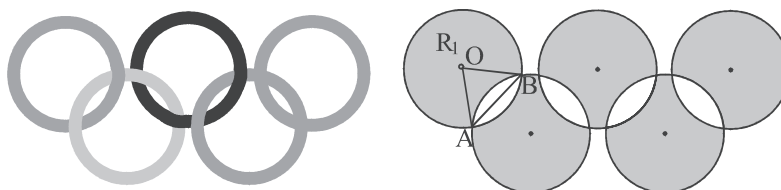
OR

- (b) How long (in seconds) will the ambulance take to reach point P from a point T on the highway such that angle of depression of the ambulance at T is 60° from the drone ?

2

37. The Olympic symbol comprising five interlocking rings represents the union of the five continents of the world and the meeting of athletes from all over the world at the Olympic games. In order to spread awareness about Olympic games, students of Class-X took part in various activities organised by the school. One such group of students made 5 circular rings in the school lawn with the help of ropes. Each circular ring required 44 m of rope.

Also, in the shaded regions as shown in the figure, students made rangoli showcasing various sports and games. It is given that $\triangle OAB$ is an equilateral triangle and all unshaded regions are congruent.



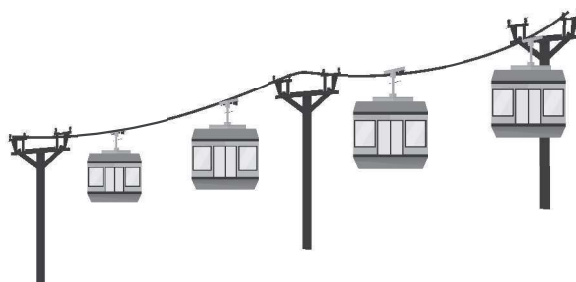
Based on above information, answer the following questions :

- (i) Find the radius of each circular ring. 1
- (ii) What is the measure of $\angle AOB$? 1
- (iii) (a) Find the area of shaded region R_1 . 2

OR

- (iii) (b) Find the length of rope around the unshaded regions. 2

38. Cable cars at hill stations are one of the major tourist attractions. On a hill station, the length of cable car ride from base point to top most point on the hill is 5000 m. Poles are installed at equal intervals on the way to provide support to the cables on which car moves.



The distance of first pole from base point is 200 m and subsequent poles are installed at equal interval of 150 m. Further, the distance of last pole from the top is 300 m.

Based on above information, answer the following questions using Arithmetic Progression :

- (i) Find the distance of 10th pole from the base. 1
- (ii) Find the distance between 15th pole and 25th pole. 1
- (iii) (a) Find the time taken by cable car to reach 15th pole from the top if it is moving at the speed of 5m/sec and coming from top. 2

OR

- (iii) (b) Find the total number of poles installed along the entire journey. 2