

SET~3

प्रश्न-पत्र कोड
Q.P. Code **30/3/3**

परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।
Candidates must write the Q.P. Code on the title page of the answer-book.

NOTE

- (I) Please check that this question paper contains **23** printed pages.
- (II) Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
- (III) Please check that this question paper contains **38** questions.
- (IV) **Please write down the Serial Number of the question in the answer-book at the given place before attempting it.**
- (V) 15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the candidates will read the question paper only and will not write any answer on the answer-book during this period.

MATHEMATICS (STANDARD)

Time allowed : 3 hours

Maximum Marks : 80

General Instructions :

Read the following instructions very carefully and strictly follow them :

- (i) *This question paper contains **38** questions. **All** questions are **compulsory**.*
- (ii) *This question paper is divided into **five** Sections – **A, B, C, D** and **E**.*
- (iii) *In **Section A**, Questions no. **1** to **18** are Multiple Choice Questions (MCQs) and questions number **19** and **20** are Assertion-Reason based questions of **1** mark each.*
- (iv) *In **Section B**, Questions no. **21** to **25** are Very Short Answer (VSA) type questions, carrying **2** marks each.*
- (v) *In **Section C**, Questions no. **26** to **31** are Short Answer (SA) type questions, carrying **3** marks each.*
- (vi) *In **Section D**, Questions no. **32** to **35** are Long Answer (LA) type questions carrying **5** marks each.*
- (vii) *In **Section E**, Questions no. **36** to **38** are Case Study based questions carrying **4** marks each. Internal choice is provided in **2** marks questions in each case study.*
- (viii) *There is no overall choice. However, an internal choice has been provided in 2 questions in Section B, 2 questions in Section C, 2 questions in Section D and 3 questions in Section E.*
- (ix) *Draw neat diagrams wherever required. Take $\pi = \frac{22}{7}$ wherever required, if not stated.*
- (x) *Use of calculator is **not** allowed.*

SECTION A

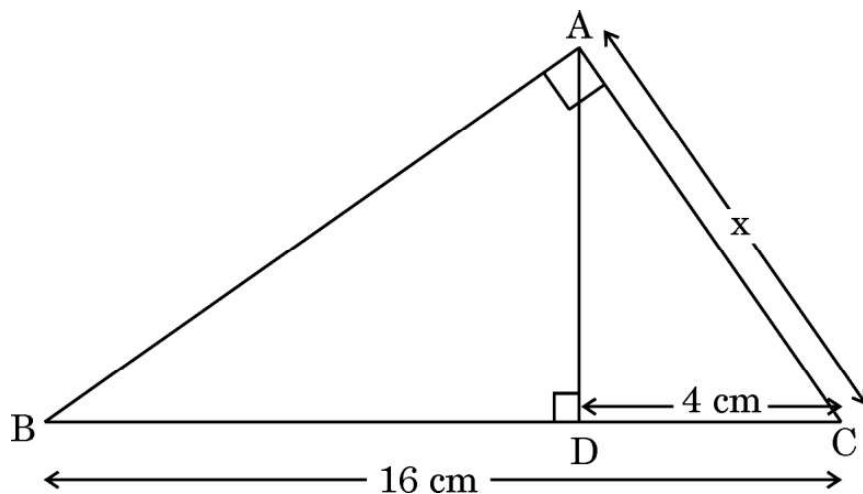
*This section has **20** Multiple Choice Questions (MCQs) carrying **1** mark each.* $20 \times 1 = 20$

1. The diameter of a wheel is 63 cm. The distance travelled by the wheel in 100 revolutions is :
(A) 99 m (B) 198 m
(C) 63 m (D) 136 m
2. The mean of seven observations is 17. If the mean of the first four observations is 15 and that of the last four observations is 18, then the fourth observation is :
(A) 14 (B) 13
(C) 12 (D) 10

3. बिंदु (4, 0) की x-अक्ष से दूरी है :
- (A) 4 इकाई (B) 16 इकाई
(C) 0 इकाई (D) $4\sqrt{2}$ इकाई
4. यदि α तथा β बहुपद $p(x) = kx^2 - 30x + 45k$ के शून्यक हैं तथा $\alpha + \beta = \alpha\beta$ है, तो 'k' का मान है :
- (A) $-\frac{2}{3}$ (B) $-\frac{3}{2}$
(C) $\frac{3}{2}$ (D) $\frac{2}{3}$
5. एक गोले की त्रिज्या 'r', एक शंकु के आधार की त्रिज्या के समान है। यदि उनके आयतन भी समान हैं, तो शंकु की ऊँचाई है :
- (A) r (B) 2r
(C) 3r (D) 4r
6. यदि किसी लाटरी में, 10 स्थानों पर इनाम हैं तथा 30 स्थान खाली हैं, तो एक इनाम जीतने की प्रायिकता है :
- (A) $\frac{1}{4}$ (B) $\frac{1}{3}$
(C) $\frac{3}{4}$ (D) $\frac{2}{3}$
7. यदि $\tan 3\theta = \sqrt{3}$ है, तो $\frac{\theta}{2}$ बराबर है :
- (A) 60° (B) 30°
(C) 20° (D) 10°
8. यदि दो त्रिभुजों $\triangle DEF$ तथा $\triangle PQR$ में, $\angle D = \angle Q$ तथा $\angle R = \angle E$ है, तो निम्नलिखित में से कौन-सा सही नहीं है ?
- (A) $\frac{DE}{QR} = \frac{DF}{PQ}$ (B) $\frac{EF}{PR} = \frac{DF}{PQ}$
(C) $\frac{EF}{RP} = \frac{DE}{QR}$ (D) $\frac{DE}{PQ} = \frac{EF}{RP}$

3. The distance of the point (4, 0) from x-axis is :
- (A) 4 units (B) 16 units
(C) 0 units (D) $4\sqrt{2}$ units
4. If α and β are zeroes of the polynomial $p(x) = kx^2 - 30x + 45k$ and $\alpha + \beta = \alpha\beta$, then the value of 'k' is :
- (A) $-\frac{2}{3}$ (B) $-\frac{3}{2}$
(C) $\frac{3}{2}$ (D) $\frac{2}{3}$
5. The radii 'r' of a sphere and that of the base of a cone are same. If their volumes are also same, then the height of the cone is :
- (A) r (B) 2r
(C) 3r (D) 4r
6. If in a lottery, there are 10 prizes and 30 blanks, then the probability of winning a prize is :
- (A) $\frac{1}{4}$ (B) $\frac{1}{3}$
(C) $\frac{3}{4}$ (D) $\frac{2}{3}$
7. If $\tan 3\theta = \sqrt{3}$, then $\frac{\theta}{2}$ equals :
- (A) 60° (B) 30°
(C) 20° (D) 10°
8. If in two triangles ΔDEF and ΔPQR , $\angle D = \angle Q$ and $\angle R = \angle E$, then which of the following is **not** true ?
- (A) $\frac{DE}{QR} = \frac{DF}{PQ}$ (B) $\frac{EF}{PR} = \frac{DF}{PQ}$
(C) $\frac{EF}{RP} = \frac{DE}{QR}$ (D) $\frac{DE}{PQ} = \frac{EF}{RP}$

9. दी गई आकृति में, $\triangle ABC$ में, $AD \perp BC$ तथा $\angle BAC = 90^\circ$ है। यदि $BC = 16$ cm तथा $DC = 4$ cm है, तो x का मान है :



- (A) 4 cm (B) 5 cm
(C) 8 cm (D) 3 cm
10. $\triangle PQR$ के दो शीर्ष $P(-1, 5)$ तथा $Q(5, 2)$ हैं। रेखाखण्ड PQ को 2 : 1 के अनुपात में बाँटने वाले बिंदु के निर्देशांक हैं :

- (A) $(3, -3)$
(B) $(5, 5)$
(C) $(3, 3)$
(D) $(5, 1)$

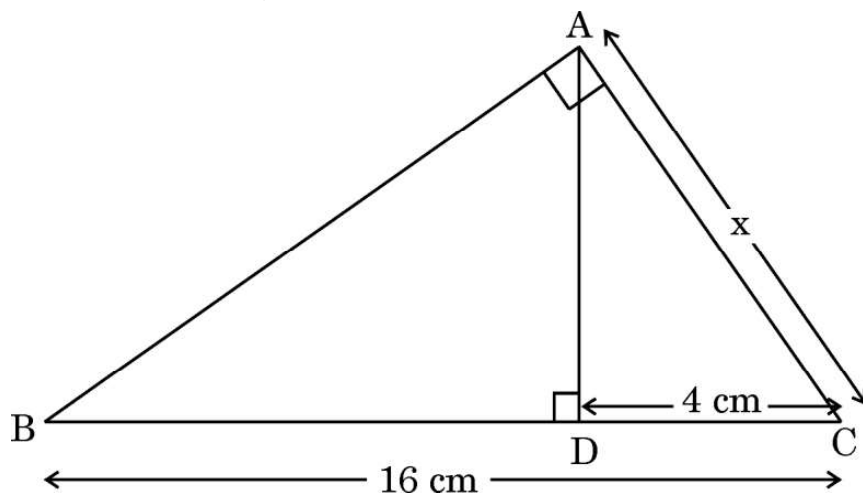
11. $(\cot \theta + \tan \theta)$ बराबर है :

- (A) $\operatorname{cosec} \theta \sec \theta$ (B) $\sin \theta \sec \theta$
(C) $\cos \theta \tan \theta$ (D) $\sin \theta \cos \theta$

12. बहुपद $p(x) = x^2 - 3\sqrt{2}x + 4$ के शून्यक हैं :

- (A) $2, \sqrt{2}$
(B) $2\sqrt{2}, \sqrt{2}$
(C) $4\sqrt{2}, -\sqrt{2}$
(D) $\sqrt{2}, 2$

- 9.** In the given figure, in $\triangle ABC$, $AD \perp BC$ and $\angle BAC = 90^\circ$. If $BC = 16$ cm and $DC = 4$ cm, then the value of x is :

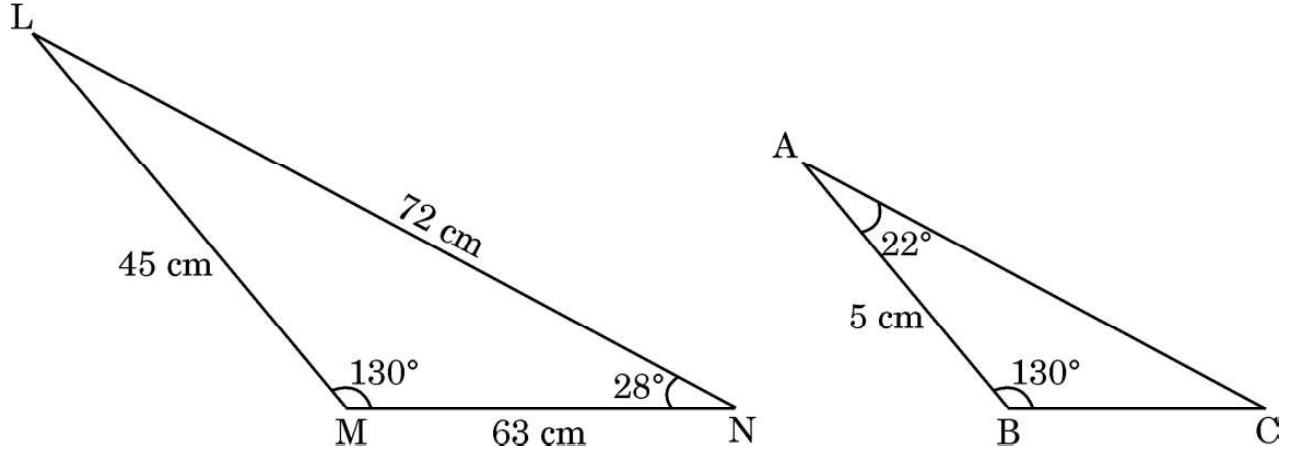


- (A) 4 cm (B) 5 cm
(C) 8 cm (D) 3 cm
10. Two of the vertices of ΔPQR are $P(-1, 5)$ and $Q(5, 2)$. The coordinates of a point which divides PQ in the ratio $2 : 1$ are :
- (A) $(3, -3)$
(B) $(5, 5)$
(C) $(3, 3)$
(D) $(5, 1)$
11. $(\cot \theta + \tan \theta)$ equals :
- (A) $\operatorname{cosec} \theta \sec \theta$ (B) $\sin \theta \sec \theta$
(C) $\cos \theta \tan \theta$ (D) $\sin \theta \cos \theta$
12. Zeroes of the polynomial $p(x) = x^2 - 3\sqrt{2}x + 4$ are :
- (A) $2, \sqrt{2}$
(B) $2\sqrt{2}, \sqrt{2}$
(C) $4\sqrt{2}, -\sqrt{2}$
(D) $\sqrt{2}, 2$

13. 'k' का वह मान जिसके लिए रैखिक समीकरण निकाय $6x + y = 3k$ तथा $36x + 6y = 3$ के अपरिमित रूप से अनेक हल हैं, है :

- (A) 6 (B) $\frac{1}{6}$
(C) $\frac{1}{2}$ (D) $\frac{1}{3}$

14. नीचे दी गई आकृति में दो त्रिभुजों LMN तथा ABC के माप दिए गए हैं। भुजा AC की लंबाई है :



- (A) 16 cm (B) 7 cm
(C) 8 cm (D) 4 cm

15. $\frac{x}{4} + \frac{y}{6} = 1$ द्वारा निरूपित रेखा, x-अक्ष तथा y-अक्ष को क्रमशः P तथा Q पर काटती है। रेखाखण्ड PQ के मध्य-बिंदु के निर्देशांक हैं :

- (A) (2, 3) (B) (3, 2)
(C) (2, 0) (D) (0, 3)

16. यदि 4, 6, 8 का ल.स. (LCM) x है, 3, 5, 7 का ल.स. y है तथा x और y का ल.स. p है, तो निम्नलिखित में से कौन-सा सही है ?

- (A) $p = 35x$ (B) $p = 4y$
(C) $p = 8x$ (D) $p = 16y$

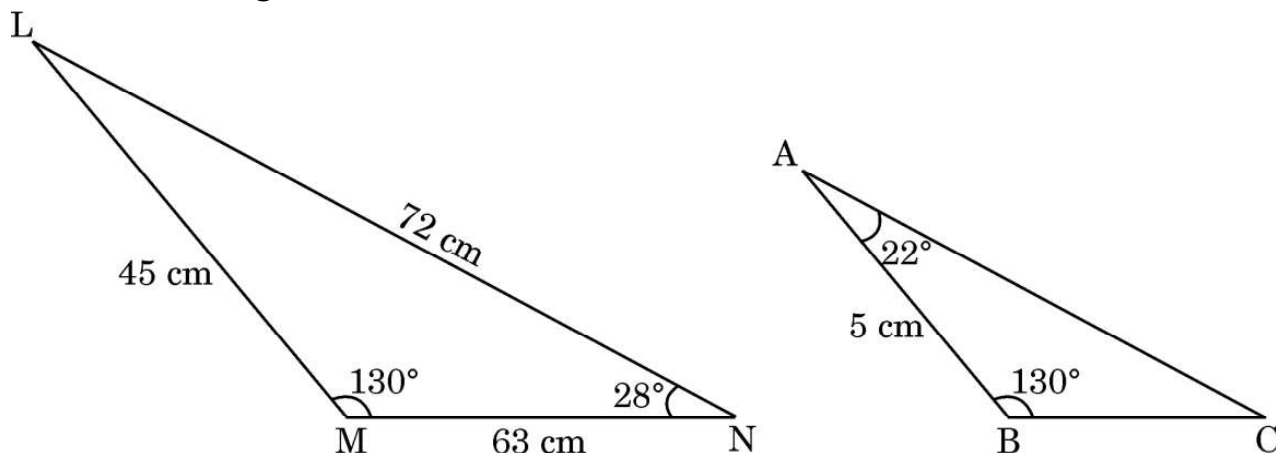
17. यदि $\frac{x}{12} - \frac{3}{x} = 0$ है, तो x के मान हैं :

- (A) ± 6 (B) ± 4
(C) ± 12 (D) ± 3

13. The value of 'k' for which the system of linear equations $6x + y = 3k$ and $36x + 6y = 3$ have infinitely many solutions is :

(A) 6 (B) $\frac{1}{6}$
(C) $\frac{1}{2}$ (D) $\frac{1}{3}$

14. The measurements of $\triangle LMN$ and $\triangle ABC$ are shown in the figure given below. The length of side AC is :



(A) 16 cm (B) 7 cm
(C) 8 cm (D) 4 cm

15. The line represented by $\frac{x}{4} + \frac{y}{6} = 1$, intersects x-axis and y-axis respectively at P and Q. The coordinates of the mid-point of line segment PQ are :

(A) (2, 3) (B) (3, 2)
(C) (2, 0) (D) (0, 3)

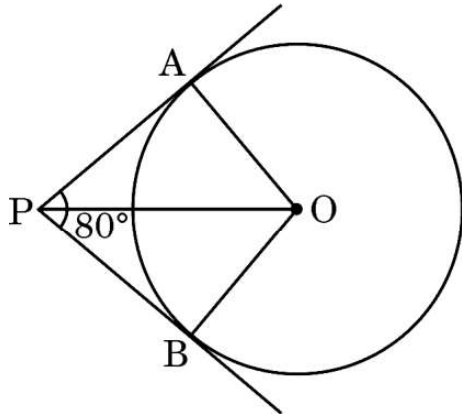
16. If x is the LCM of 4, 6, 8 and y is the LCM of 3, 5, 7 and p is the LCM of x and y, then which of the following is true ?

(A) $p = 35x$ (B) $p = 4y$
(C) $p = 8x$ (D) $p = 16y$

17. If $\frac{x}{12} - \frac{3}{x} = 0$, then the values of x are :

(A) ± 6 (B) ± 4
(C) ± 12 (D) ± 3

18. If tangents PA and PB drawn from an external point P to the circle with centre O are inclined to each other at an angle of 80° as shown in the given figure, then the measure of $\angle POA$ is :



- | | |
|----------------|----------------|
| (A) 40° | (B) 50° |
| (C) 60° | (D) 80° |

Questions number 19 and 20 are Assertion and Reason based questions. Two statements are given, one labelled as Assertion (A) and the other is labelled as Reason (R). Select the correct answer to these questions from the codes (A), (B), (C) and (D) as given below.

- (A) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of the Assertion (A).
- (B) Both Assertion (A) and Reason (R) are true, but Reason (R) is **not** the correct explanation of the Assertion (A).
- (C) Assertion (A) is true, but Reason (R) is false.
- (D) Assertion (A) is false, but Reason (R) is true.
19. *Assertion (A)* : If two tangents are drawn to a circle from an external point, then they subtend equal angles at the centre of the circle.
- Reason (R)*: A parallelogram circumscribing a circle is a rhombus.
20. *Assertion (A)* : A ladder leaning against a wall, stands at a horizontal distance of 6 m from the wall. If the height of the wall up to which the ladder reaches is 8 m, then the length of the ladder is 10 m.
- Reason (R)*: The ladder makes an angle of 60° with the ground.

SECTION B

This section has 5 Very Short Answer (VSA) type questions carrying 2 marks each. 5×2=10

21. If $\tan A + \cot A = 6$, then find the value of $\tan^2 A + \cot^2 A - 4$.
22. (a) Find the value(s) of 'k' so that the quadratic equation $4x^2 + kx + 1 = 0$ has real and equal roots.

OR

- (b) If ' α ' and ' β ' are the zeroes of the polynomial $p(y) = y^2 - 5y + 3$, then find the value of $\alpha^4\beta^3 + \alpha^3\beta^4$.
23. The probability of guessing the correct answer of a certain test question is $\frac{x}{12}$. If the probability of not guessing the correct answer is $\frac{5}{6}$, then find the value of x.
24. Prove that the tangents drawn at the ends of a diameter of a circle are parallel.
25. (a) Find the smallest number which is divisible by both 644 and 462.

OR

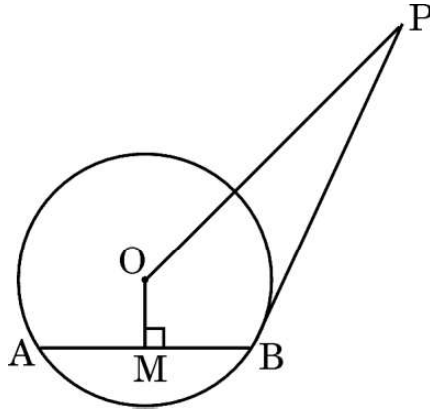
- (b) Two numbers are in the ratio 4 : 5 and their HCF is 11. Find the LCM of these numbers.

SECTION C

This section has 6 Short Answer (SA) type questions carrying 3 marks each. 6×3=18

26. All face cards of spades are removed from a pack of 52 playing cards and the remaining pack is shuffled well. A card is then drawn at random from the remaining pack. Find the probability of getting :
- (a) a face card
- (b) an ace or a jack

27. In the given figure, PB is a tangent to the circle with centre O at B. AB is a chord of the circle of length 24 cm and at a distance of 5 cm from the centre of the circle. If the length PB of the tangent is 20 cm, find the length of OP.



28. A chord of a circle of radius 10 cm subtends a right angle at the centre of the circle. Find the area of the corresponding minor segment. [Use $\pi = 3.14$]

29. Prove that $\left(5\sqrt{3} + \frac{2}{3}\right)$ is an irrational number given that $\sqrt{3}$ is an irrational number.

30. (a) Prove that : $\sqrt{\frac{\sec A - 1}{\sec A + 1}} + \sqrt{\frac{\sec A + 1}{\sec A - 1}} = 2 \operatorname{cosec} A$

OR

- (b) Prove that : $\left(\frac{1}{\cos A} - \cos A\right)\left(\frac{1}{\sin A} - \sin A\right) = \frac{1}{\tan A + \cot A}$

31. (a) If the mid-point of the line segment joining the points A(3, 4) and B(k, 6) is P(x, y) and $x + y - 10 = 0$, find the value of k.

OR

- (b) Find the coordinates of the points which divide the line segment joining A(-2, 2) and B(2, 8) into four equal parts.

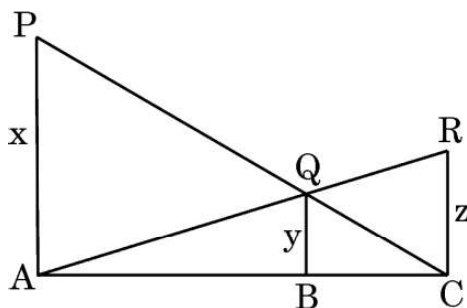
SECTION D

This section has 4 Long Answer (LA) type questions carrying 5 marks each. 4×5=20

- 32.** A solid toy is in the form of a hemisphere surmounted by a right circular cone. The height of the cone is 2 cm and the diameter of the base is 4 cm. Determine the volume of the toy. Also, find the surface area of the toy. (Take $\pi = 3.14$)
- 33.** The students of a class are made to stand equally in rows. If 3 students are extra in each row, there would be 1 row less. If 3 students are less in a row, there would be 2 more rows. Find the number of students in the class.
- 34.** (a) The sum of the third term and the seventh term of an AP is 6 and their product is 8. Find the sum of the first sixteen terms of the AP.

OR

- (b) The minimum age of children eligible to participate in a painting competition is 8 years. It is observed that the age of the youngest boy was 8 years and the ages of the participants, when seated in order of age, have a common difference of 4 months. If the sum of the ages of all the participants is 168 years, find the age of the eldest participant in the painting competition.
- 35.** (a) In the given figure, PA, QB and RC are perpendicular to AC. If $PA = x$ units, $QB = y$ units and $RC = z$ units, prove that $\frac{1}{x} + \frac{1}{z} = \frac{1}{y}$.



OR

- (b) Sides AB and BC and median AD of triangle ABC are respectively proportional to sides PQ and QR and median PM of $\triangle PQR$. Show that $\triangle ABC \sim \triangle PQR$.

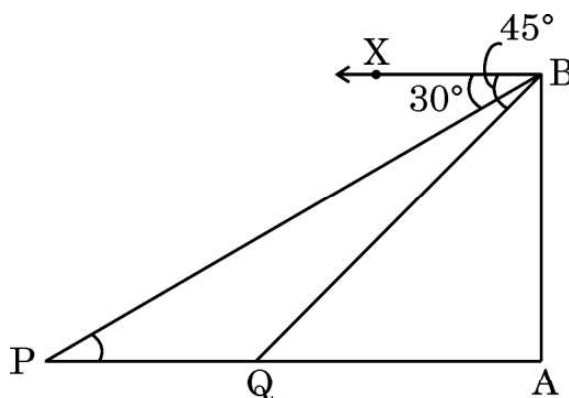
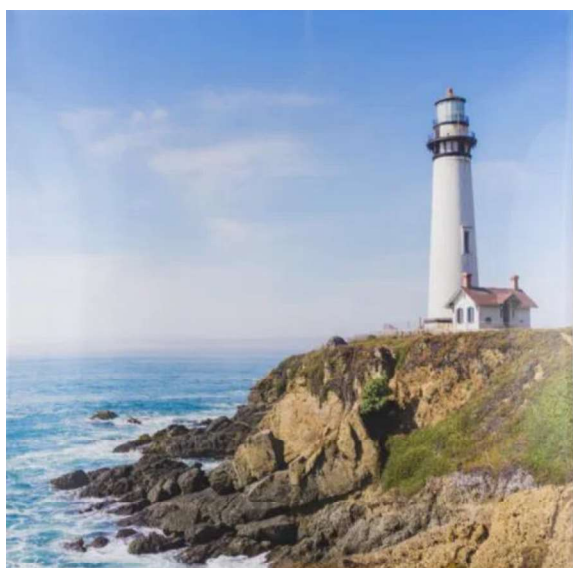
SECTION E

This section has 3 Case Study based questions carrying 4 marks each.

$3 \times 4 = 12$

Case Study – 1

36. A lighthouse stands tall on a cliff by the sea, watching over ships that pass by. One day a ship is seen approaching the shore and from the top of the lighthouse, the angles of depression of the ship are observed to be 30° and 45° as it moves from point P to point Q. The height of the lighthouse is 50 metres.



Based on the information given above, answer the following questions :

- (i) Find the distance of the ship from the base of the lighthouse when it is at point Q, where the angle of depression is 45° . 1
- (ii) Find the measures of $\angle PBA$ and $\angle QBA$. 1
- (iii) (a) Find the distance travelled by the ship between points P and Q. 2

OR

- (b) If the ship continues moving towards the shore and takes 10 minutes to travel from Q to A, calculate the speed of the ship in km/h, from Q to A. 2

Case Study – 2

37. The India Meteorological Department observes seasonal and annual rainfall every year in different sub-divisions of our country. It helps them to compare and analyse the results.



The table below shows sub-divisions wise seasonal (monsoon) rainfall (in mm) in 2023.

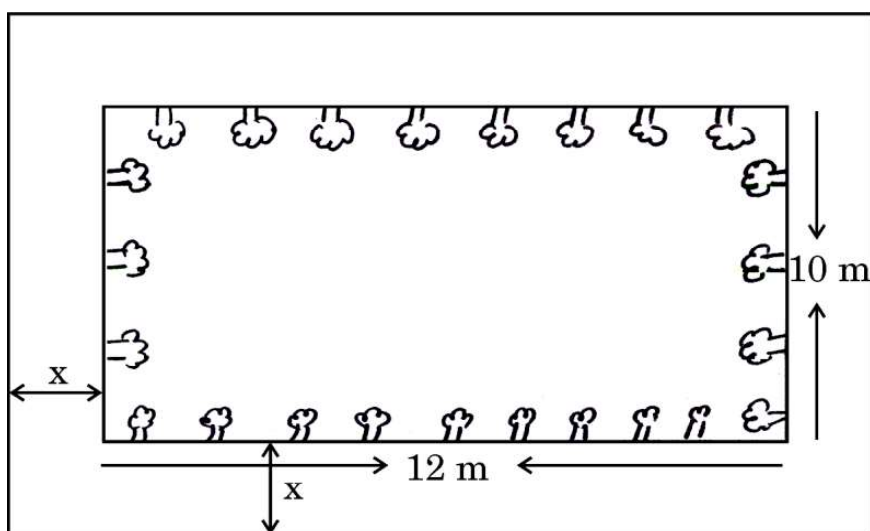
<i>Rainfall (mm)</i>	<i>No. of Sub-divisions</i>
200 – 400	3
400 – 600	4
600 – 800	7
800 – 1000	4
1000 – 1200	3
1200 – 1400	3

Based on the information given above, answer the following questions :

- (i) Write the modal class. 1
- (ii) (a) Find the median of the given data. 2
- OR**
- (b) Find the mean rainfall in the season. 2
- (iii) If a sub-division having at least 800 mm rainfall during monsoon season is considered a good rainfall sub-division, then how many sub-divisions had good rainfall ? 1

Case Study – 3

38. A garden designer is planning a rectangular lawn that is to be surrounded by a uniform walkway.



The total area of the lawn and the walkway is 360 square metres. The width of the walkway is same on all sides. The dimensions of the lawn itself are 12 metres by 10 metres.

Based on the information given above, answer the following questions :

- (i) Formulate the quadratic equation representing the total area of the lawn and the walkway, taking width of walkway = x m. 1
- (ii) (a) Solve the quadratic equation to find the width of the walkway ' x '. 2

OR

- (b) If the cost of paving the walkway at the rate of ₹ 50 per square metre is ₹ 12,000, calculate the area of the walkway. 2
- (iii) Find the perimeter of the lawn. 1