

Series : GE1FH



SET~1

रोल नं.
Roll No.



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- (I) कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृष्ठ **27** हैं।
- (II) प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए प्रश्न-पत्र कोड को परीक्षार्थी उत्तर-पुस्तिका के मुख-पृष्ठ पर लिखें।
- (III) कृपया जाँच कर लें कि इस प्रश्न-पत्र में **38** प्रश्न हैं।
- (IV) कृपया प्रश्न का उत्तर लिखना शुरू करने से पहले, उत्तर-पुस्तिका में यथा स्थान पर प्रश्न का क्रमांक अवश्य लिखें।
- (V) इस प्रश्न-पत्र को पढ़ने के लिए 15 मिनट का समय दिया गया है। प्रश्न-पत्र का वितरण पूर्वाह्न में 10.15 बजे किया जाएगा। 10.15 बजे से 10.30 बजे तक परीक्षार्थी केवल प्रश्न-पत्र को पढ़ेंगे और इस अवधि के दौरान वे उत्तर-पुस्तिका पर कोई उत्तर नहीं लिखेंगे।

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प्रश्न-पत्र कोड
Q.P. Code **30/1/1**

परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।

Candidates must write the Q.P. Code on the title page of the answer-book.

NOTE

- (I) Please check that this question paper contains **27** printed pages.
- (II) Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
- (III) Please check that this question paper contains **38** questions.
- (IV) Please write down the Serial Number of the question in the answer-book at the given place before attempting it.
- (V) 15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the candidates will read the question paper only and will not write any answer on the answer-book during this period.



गणित (मानक)

MATHEMATICS (STANDARD)

निर्धारित समय : 3 घण्टे

Time allowed : 3 hours

अधिकतम अंक : 80

Maximum Marks : 80



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General Instructions :

Read the following instructions very carefully and strictly follow them :

- (i) *This question paper contains **38** questions. **All** questions are **compulsory**.*
- (ii) *This question paper is divided into **five** Sections – **A, B, C, D** and **E**.*
- (iii) *In **Section A**, Questions no. **1** to **18** are multiple choice questions (MCQs) and questions number **19** and **20** are Assertion-Reason based questions of **1** mark each.*
- (iv) *In **Section B**, Questions no. **21** to **25** are very short answer (VSA) type questions, carrying **2** marks each.*
- (v) *In **Section C**, Questions no. **26** to **31** are short answer (SA) type questions, carrying **3** marks each.*
- (vi) *In **Section D**, Questions no. **32** to **35** are long answer (LA) type questions carrying **5** marks each.*
- (vii) *In **Section E**, Questions no. **36** to **38** are case study based questions carrying **4** marks each. Internal choice is provided in **2** marks questions in each case study.*
- (viii) *There is no overall choice. However, an internal choice has been provided in **2** questions in Section B, **2** questions in Section C, **2** questions in Section D and **3** questions in Section E.*
- (ix) *Draw neat diagrams wherever required. Take $\pi = \frac{22}{7}$ wherever required, if not stated.*
- (x) *Use of calculator is **not** allowed.*

SECTION A

*This section has **20** Multiple Choice Questions (MCQs) carrying **1** mark each. $20 \times 1 = 20$*

1. If α and β are the zeroes of polynomial $3x^2 + 6x + k$ such that $\alpha + \beta + \alpha\beta = -\frac{2}{3}$, then the value of k is :
- (A) -8
 - (B) 8
 - (C) -4
 - (D) 4



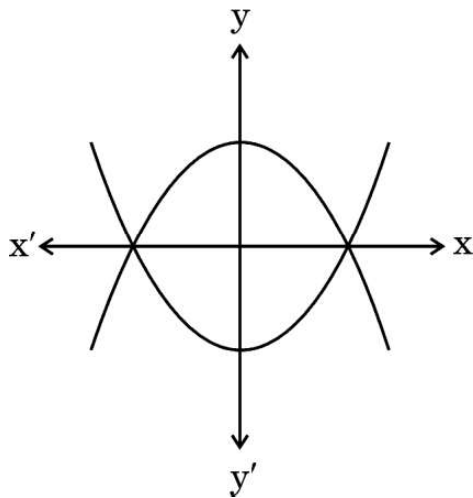
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2. If $x = 1$ and $y = 2$ is a solution of the pair of linear equations $2x - 3y + a = 0$ and $2x + 3y - b = 0$, then :
- (A) $a = 2b$
(B) $2a = b$
(C) $a + 2b = 0$
(D) $2a + b = 0$
3. The mid-point of the line segment joining the points $P(-4, 5)$ and $Q(4, 6)$ lies on :
- (A) x-axis
(B) y-axis
(C) origin
(D) neither x-axis nor y-axis
4. If θ is an acute angle and $7 + 4 \sin \theta = 9$, then the value of θ is :
- (A) 90°
(B) 30°
(C) 45°
(D) 60°
5. The value of $\tan^2 \theta - \left(\frac{1}{\cos \theta} \times \sec \theta \right)$ is :
- (A) 1
(B) 0
(C) -1
(D) 2
6. If $\text{HCF}(98, 28) = m$ and $\text{LCM}(98, 28) = n$, then the value of $n - 7m$ is :
- (A) 0
(B) 28
(C) 98
(D) 198



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7. The tangents drawn at the extremities of the diameter of a circle are always :
- (A) parallel
 - (B) perpendicular
 - (C) equal
 - (D) intersecting
8. In triangles ABC and DEF, $\angle B = \angle E$, $\angle F = \angle C$ and $AB = 3 DE$. Then, the two triangles are :
- (A) congruent but not similar
 - (B) congruent as well as similar
 - (C) neither congruent nor similar
 - (D) similar but not congruent
9. If $(-1)^n + (-1)^8 = 0$, then n is :
- (A) any positive integer
 - (B) any negative integer
 - (C) any odd number
 - (D) any even number
10. Two polynomials are shown in the graph below. The number of distinct zeroes of both the polynomials is :



- | | |
|-------|-------|
| (A) 3 | (B) 5 |
| (C) 2 | (D) 4 |



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11. If the sum of first m terms of an AP is $2m^2 + 3m$, then its second term is :
- (A) 10
(B) 9
(C) 12
(D) 4
12. Mode and Mean of a data are $15x$ and $18x$, respectively. Then the median of the data is :
- (A) x
(B) $11x$
(C) $17x$
(D) $34x$
13. A card is selected at random from a deck of 52 playing cards. The probability of it being a red face card is :
- (A) $\frac{3}{13}$
(B) $\frac{2}{13}$
(C) $\frac{1}{2}$
(D) $\frac{3}{26}$
14. Which of the following is a rational number between $\sqrt{3}$ and $\sqrt{5}$?
- (A) $1.4142387954012 \dots$
(B) $2.\overline{326}$
(C) π
(D) 1.857142

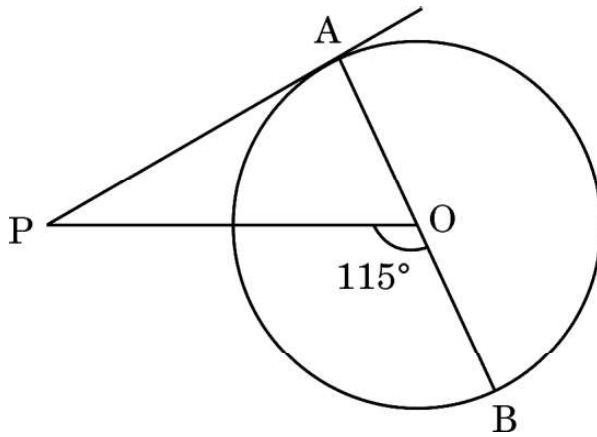


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15. If a sector of a circle has an area of 40π sq. units and a central angle of 72° , the radius of the circle is :

- (A) 200 units
- (B) 100 units
- (C) 20 units
- (D) $10\sqrt{2}$ units

16. In the given figure, PA is a tangent from an external point P to a circle with centre O. If $\angle POB = 115^\circ$, then $\angle APO$ is equal to :



- (A) 25°
- (B) 65°
- (C) 90°
- (D) 35°

17. A kite is flying at a height of 150 m from the ground. It is attached to a string inclined at an angle of 30° to the horizontal. The length of the string is :

- (A) $100\sqrt{3}$ m
- (B) 300 m
- (C) $150\sqrt{2}$ m
- (D) $150\sqrt{3}$ m



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18. A piece of wire 20 cm long is bent into the form of an arc of a circle of radius $\frac{60}{\pi}$ cm. The angle subtended by the arc at the centre of the circle is :
- (A) 30°
(B) 60°
(C) 90°
(D) 50°

Questions number 19 and 20 are Assertion and Reason based questions. Two statements are given, one labelled as Assertion (A) and the other is labelled as Reason (R). Select the correct answer to these questions from the codes (A), (B), (C) and (D) as given below.

- (A) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of the Assertion (A).
(B) Both Assertion (A) and Reason (R) are true, but Reason (R) is **not** the correct explanation of the Assertion (A).
(C) Assertion (A) is true, but Reason (R) is false.
(D) Assertion (A) is false, but Reason (R) is true.
19. *Assertion (A) :* The probability of selecting a number at random from the numbers 1 to 20 is 1.
Reason (R): For any event E, if $P(E) = 1$, then E is called a sure event.
20. *Assertion (A) :* If we join two hemispheres of same radius along their bases, then we get a sphere.
Reason (R): Total Surface Area of a sphere of radius r is $3\pi r^2$.



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SECTION B

This section has 5 Very Short Answer (VSA) type questions carrying 2 marks each. 5×2=10

21. (a) If $x \cos 60^\circ + y \cos 0^\circ + \sin 30^\circ - \cot 45^\circ = 5$, then find the value of $x + 2y$.

OR

- (b) Evaluate : $\frac{\tan^2 60^\circ}{\sin^2 60^\circ + \cos^2 30^\circ}$

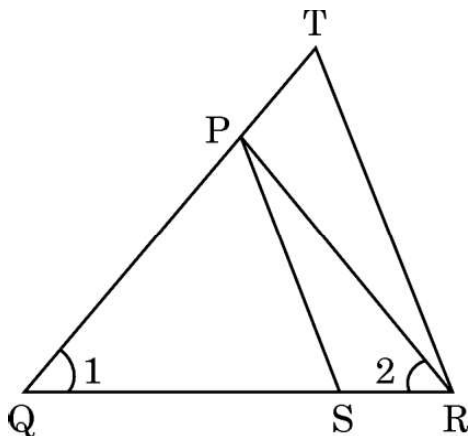
22. Find the zeroes of the polynomial $p(x) = x^2 + \frac{4}{3}x - \frac{4}{3}$.

23. The coordinates of the centre of a circle are $(2a, a - 7)$. Find the value(s) of 'a' if the circle passes through the point $(11, -9)$ and has diameter $10\sqrt{2}$ units.

24. (a) If $\Delta ABC \sim \Delta PQR$ in which $AB = 6$ cm, $BC = 4$ cm, $AC = 8$ cm and $PR = 6$ cm, then find the length of $(PQ + QR)$.

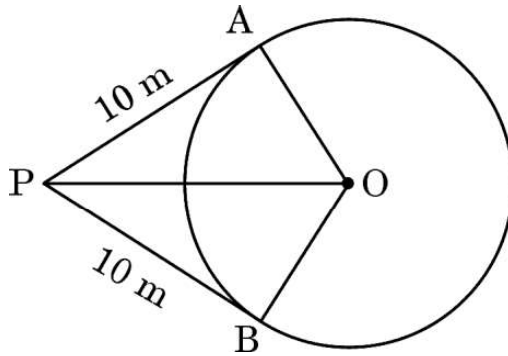
OR

- (b) In the given figure, $\frac{QR}{QS} = \frac{QT}{PR}$ and $\angle 1 = \angle 2$, show that $\Delta PQS \sim \Delta TQR$.



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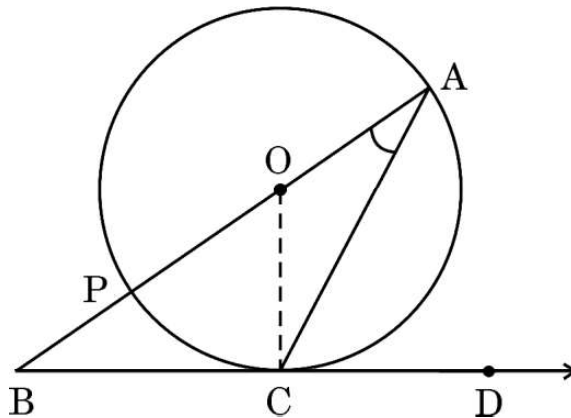
25. A person is standing at P outside a circular ground at a distance of 26 m from the centre of the ground. He found that his distances from the points A and B on the ground are 10 m (PA and PB are tangents to the circle). Find the radius of the circular ground.



SECTION C

This section has 6 Short Answer (SA) type questions carrying 3 marks each. $6 \times 3 = 18$

26. (a) In the given figure, O is the centre of the circle and BCD is tangent to it at C. Prove that $\angle BAC + \angle ACD = 90^\circ$.



OR

- (b) Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre of the circle.



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27. (a) Prove that : $\frac{\tan \theta}{1 - \cot \theta} + \frac{\cot \theta}{1 - \tan \theta} = 1 + \sec \theta \operatorname{cosec} \theta$

OR

(b) Prove that : $\frac{\sin A + \cos A}{\sin A - \cos A} + \frac{\sin A - \cos A}{\sin A + \cos A} = \frac{2}{2 \sin^2 A - 1}$

28. Find the ratio in which the y-axis divides the line segment joining the points (5, -6) and (-1, -4). Also find the point of intersection.

29. Prove that $\frac{1}{\sqrt{5}}$ is an irrational number.

30. A room is in the form of a cylinder surmounted by a hemispherical dome. The base radius of the hemisphere is half of the height of the cylindrical part. If the room contains $\frac{1408}{21} \text{ m}^3$ of air, find the height of the cylindrical part. (Use $\pi = \frac{22}{7}$).

31. Two dice are thrown at the same time. Determine the probability that the difference of the numbers on the two dice is 2.

SECTION D

This section has 4 Long Answer (LA) type questions carrying 5 marks each. 4×5=20

32. Vijay invested certain amounts of money in two schemes A and B, which offer interest at the rate of 8% per annum and 9% per annum, respectively. He received ₹ 1,860 as the total annual interest. However, had he interchanged the amounts of investments in the two schemes, he would have received ₹ 20 more as annual interest. How much money did he invest in each scheme ?



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33. (a) The diagonal BD of a parallelogram ABCD intersects the line segment AE at the point F, where E is any point on the side BC. Prove that $DF \times EF = FB \times FA$.

OR

- (b) In $\triangle ABC$, if $AD \perp BC$ and $AD^2 = BD \times DC$, then prove that $\angle BAC = 90^\circ$.

34. (a) The perimeter of a right triangle is 60 cm and its hypotenuse is 25 cm. Find the lengths of other two sides of the triangle.

OR

- (b) A train travels a distance of 480 km at a uniform speed. If the speed had been 8 km/h less, then it would have taken 3 hours more to cover the same distance. Find the speed of the train.

35. Find the missing frequency 'f' in the following table, if the mean of the given data is 18. Hence find the mode.

<i>Daily Allowance</i>	<i>Number of Children</i>
11 – 13	7
13 – 15	6
15 – 17	9
17 – 19	13
19 – 21	f
21 – 23	5
23 – 25	4



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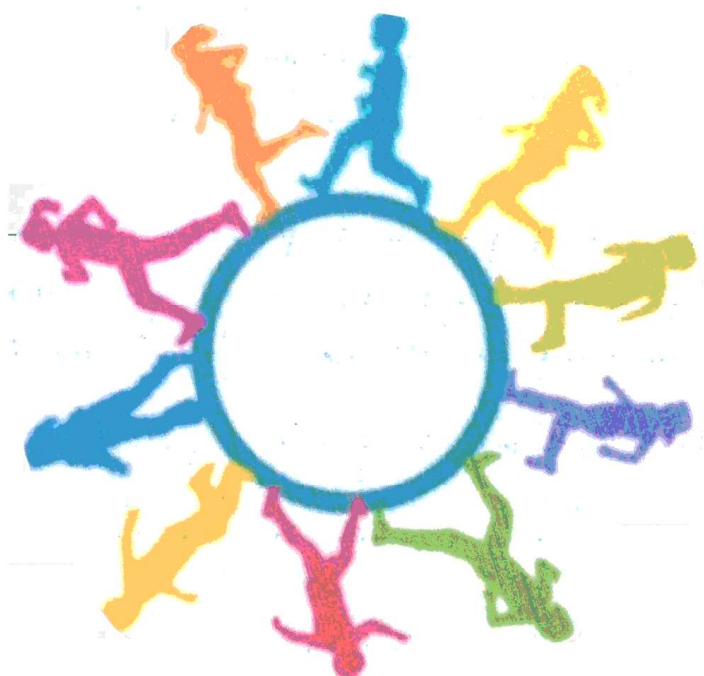
SECTION E

This section has 3 case study based questions carrying 4 marks each.

$3 \times 4 = 12$

Case Study – 1

36. A school is organizing a charity run to raise funds for a local hospital. The run is planned as a series of rounds around a track, with each round being 300 metres. To make the event more challenging and engaging, the organizers decide to increase the distance of each subsequent round by 50 metres. For example, the second round will be 350 metres, the third round will be 400 metres and so on. The total number of rounds planned is 10.



Based on the information given above, answer the following questions :

- (i) Write the fourth, fifth and sixth term of the Arithmetic Progression so formed. 1
- (ii) Determine the distance of the 8th round. 1
- (iii) (a) Find the total distance run after completing all 10 rounds. 2

OR

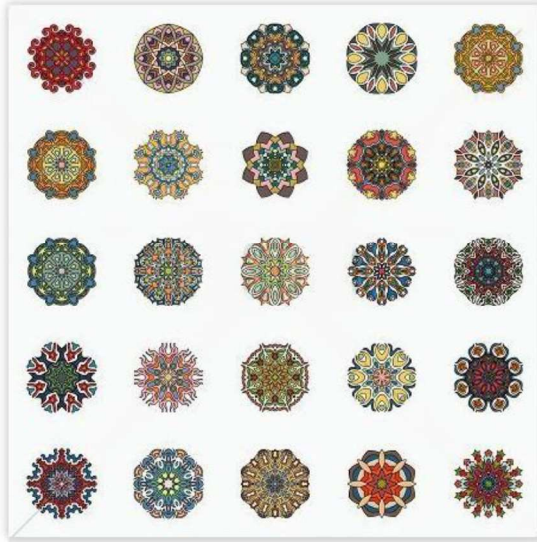
- (iii) (b) If a runner completes only the first 6 rounds, what is the total distance run by the runner ? 2



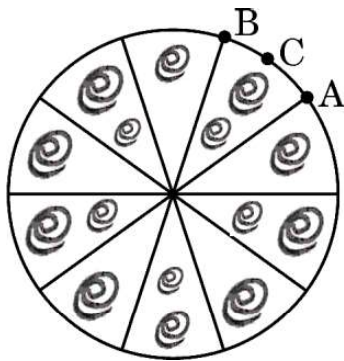
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Case Study – 2

37. A brooch is a decorative piece often worn on clothing like jackets, blouses or dresses to add elegance. Made from precious metals and decorated with gemstones, brooches come in many shapes and designs.



One such brooch is made with silver wire in the form of a circle with diameter 35 mm. The wire is also used in making 5 diameters which divide the circle into 10 equal sectors as shown in the figure.



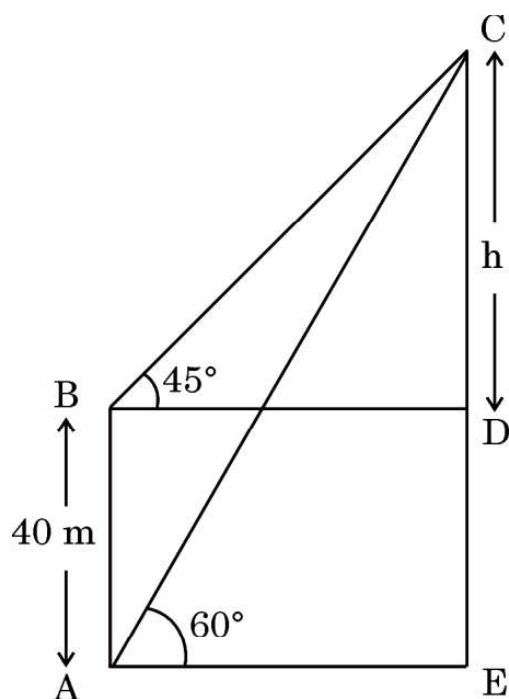
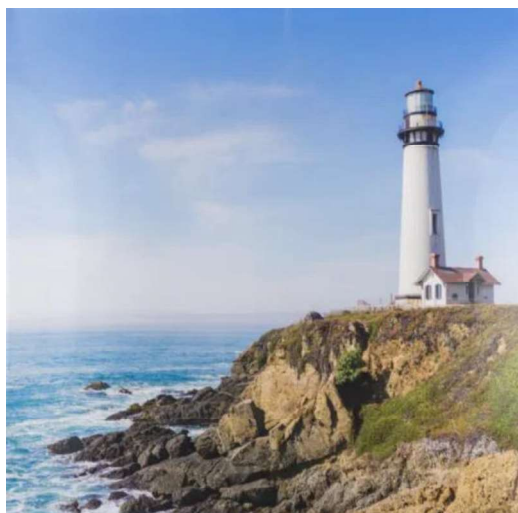
Based on the above given information, answer the following questions :

- | | | |
|-----------|--|---|
| (i) | Find the central angle of each sector. | 1 |
| (ii) | Find the length of the arc ACB. | 1 |
| (iii) | (a) Find the area of each sector of the brooch. | 2 |
| OR | | |
| (iii) | (b) Find the total length of the silver wire used. | 2 |



Case Study – 3

38. Amrita stood near the base of a lighthouse, gazing up at its towering height. She measured the angle of elevation to the top and found it to be 60° . Then, she climbed a nearby observation deck, 40 metres higher than her original position and noticed the angle of elevation to the top of lighthouse to be 45° .



Based on the above given information, answer the following questions :

- | | | |
|-----------|---|---|
| (i) | If CD is h metres, find the distance BD in terms of ' h '. | 1 |
| (ii) | Find distance BC in terms of ' h '. | 1 |
| (iii) | (a) Find the height CE of the lighthouse [Use $\sqrt{3} = 1.73$] | 2 |
| OR | | |
| (iii) | (b) Find distance AE, if AC = 100 m. | 2 |

