

**Series PPQQB/3****SET~1****प्रश्न-पत्र कोड
Q.P. Code 30/3/1**

रोल नं.

Roll No.

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परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।

Candidates must write the Q.P. Code on the title page of the answer-book.

नोट	NOTE
(I) कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृष्ठ 11 हैं।	(I) Please check that this question paper contains 11 printed pages.
(II) प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए प्रश्न-पत्र कोड को परीक्षार्थी उत्तर-पुस्तिका के मुख-पृष्ठ पर लिखें।	(II) Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
(III) कृपया जाँच कर लें कि इस प्रश्न-पत्र में 14 प्रश्न हैं।	(III) Please check that this question paper contains 14 questions.
(IV) कृपया प्रश्न का उत्तर लिखना शुरू करने से पहले, उत्तर-पुस्तिका में प्रश्न का क्रमांक अवश्य लिखें।	(IV) Please write down the serial number of the question in the answer-book before attempting it.
(V) इस प्रश्न-पत्र को पढ़ने के लिए 15 मिनट का समय दिया गया है। प्रश्न-पत्र का वितरण पूर्वाह्न में 10.15 बजे किया जाएगा। 10.15 बजे से 10.30 बजे तक छात्र केवल प्रश्न-पत्र को पढ़ेंगे और इस अवधि के दौरान वे उत्तर-पुस्तिका पर कोई उत्तर नहीं लिखेंगे।	(V) 15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the students will read the question paper only and will not write any answer on the answer-book during this period.

**गणित (मानक)****MATHEMATICS (STANDARD)**

निर्धारित समय : 2 घण्टे

अधिकतम अंक : 40

Time allowed : 2 hours

Maximum Marks : 40

**General Instructions :**

Read the following instructions very carefully and strictly follow them :

- (i) This question paper contains **14** questions. **All** questions are compulsory.
- (ii) This question paper is divided into **three** sections – **Sections A, B and C**.
- (iii) **Section A** comprises of **6** questions (Q.no. **1** to **6**) of **2** marks each. Internal choice has been provided in **two** questions.
- (iv) **Section B** comprises of **4** questions (Q.no. **7** to **10**) of **3** marks each. Internal choice has been provided in **one** question.
- (v) **Section C** comprises of **4** questions (Q.no. **11** to **14**) of **4** marks each. Internal choice has been provided in **one** question. It also contains two case study based questions.
- (vi) Use of calculator is **not** permitted.

SECTION A

Question numbers **1** to **6** carry **2** marks each.

1. (a) Solve the quadratic equation for x :

$$x^2 - 2ax - (4b^2 - a^2) = 0 \quad 2$$

OR

- (b) If the quadratic equation

$$(1 + a^2)x^2 + 2abx + (b^2 - c^2) = 0$$

has equal and real roots, then prove that :

$$b^2 = c^2 (1 + a^2) \quad 2$$

2. Find the sum of first 20 terms of an AP in which $d = 5$ and $a_{20} = 135$. 2

3. Find the mode of the given frequency distribution : 2

Class	Frequency
15 – 25	6
25 – 35	11
35 – 45	22
45 – 55	23
55 – 65	14
65 – 75	5



4. (a) 150 spherical marbles, each of diameter 1.4 cm, are dropped in a cylindrical vessel of diameter 7 cm containing some water, and are completely immersed in water. Find the rise in the level of water in the cylindrical vessel. 2

OR

- (b) Three cubes of side 6 cm each, are joined as shown in Figure 1. Find the total surface area of the resulting cuboid. 2

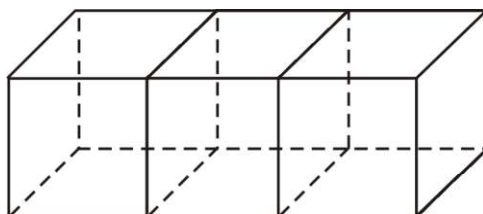


Figure 1

5. For what value of 'n', are the n^{th} terms of the APs : 9, 7, 5, and 15, 12, 9, the same ? 2
6. In Figure 2, PQ and PR are tangents to the circle centred at O. If $\angle OPR = 45^\circ$, then prove that ORPQ is a square. 2

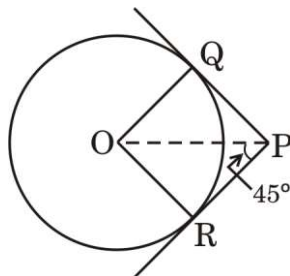


Figure 2

SECTION B

Question numbers 7 to 10 carry 3 marks each.

7. (a) Draw a line segment AB of length 8 cm and locate a point P on AB such that $AP : PB = 1 : 5$. 3

OR

- (b) Draw a circle of radius 3 cm. From a point P lying outside the circle at a distance of 6 cm from its centre, construct two tangents PA and PB to the circle. 3



8. The tops of two poles of heights 20 m and 28 m are connected with a wire. The wire is inclined to the horizontal at an angle of 30° . Find the length of the wire and the distance between the two poles. 3

9. The weights (in kg) of 50 wild animals of a National Park were recorded and the following data was obtained :

Weight (in kg)	Number of animals
100 – 110	4
110 – 120	12
120 – 130	23
130 – 140	8
140 – 150	3

Find the mean weight (in kg) of animals, using assumed mean method. 3

10. For the following frequency distribution, find the median : 3

Class	Frequency
1400 – 1550	6
1550 – 1700	13
1700 – 1850	25
1850 – 2000	10

SECTION C

Question numbers 11 to 14 carry 4 marks each.

11. (a) In Figure 3, two circles with centres at O and O' of radii 2r and r respectively, touch each other internally at A. A chord AB of the bigger circle meets the smaller circle at C. Show that C bisects AB. 4

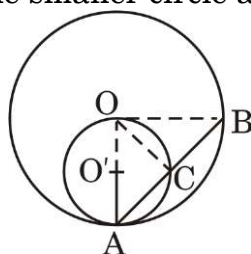


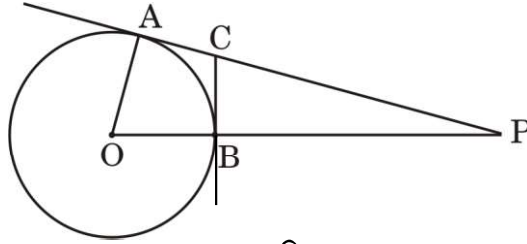
Figure 3

OR



- (ख) आकृति 4 में, 5 सेमी त्रिज्या वाले वृत्त का केंद्र बिंदु O है। PA तथा BC क्रमशः बिंदु A तथा B पर खींची गई स्पर्श-रेखाएँ हैं। यदि $OP = 13$ सेमी है, तो स्पर्श-रेखाओं PA तथा BC की लम्बाई ज्ञात कीजिए।

4



आकृति 4

12. एक सीधा राजमार्ग एक मीनार के पाद तक जाता है। मीनार के शिखर पर खड़ा एक आदमी एक कार को 30° के अवनमन कोण पर देखता है, जो कि मीनार के पाद की ओर एकसमान चाल से जा रही है। 10 सेकण्ड बाद कार का अवनमन कोण 60° हो गया। इस बिंदु से मीनार के पाद तक पहुँचने में कार द्वारा लिया गया समय ज्ञात कीजिए।

4

प्रकरण अध्ययन – 1

13. नीचे दिए गए चित्र में, एक परिवार ने अपने घर के पीछे की जमीन पर एक आयताकार स्विमिंग पूल बनवाया। पूल के चारों तरफ x मी. चौड़ा सीमेंट (कंक्रीट) से बना पक्का फुटपाथ है। फुटपाथ की बाहरी भुजाएँ 7 मी. तथा 12 मी. हैं। पूल का क्षेत्रफल 36 वर्ग मी. है।



- (क) उपर्युक्त सूचना के आधार पर x के पदों में एक द्विघात समीकरण बनाइए।
- (ख) पूल के चारों ओर बने फुटपाथ की चौड़ाई ज्ञात कीजिए।

2

2



- (b) In Figure 4, O is centre of a circle of radius 5 cm. PA and BC are tangents to the circle at A and B respectively. If $OP = 13$ cm, then find the length of tangents PA and BC.

4

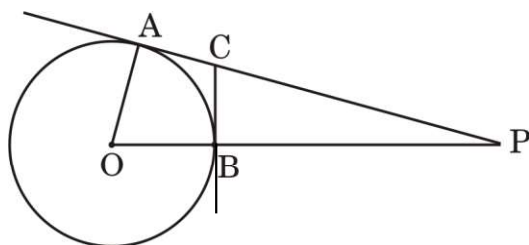


Figure 4

12. A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at an angle of depression of 30° , which is approaching the foot of the tower with a uniform speed. Ten seconds later, the angle of depression of the car is found to be 60° . Find the time taken by the car to reach the foot of the tower from this point.

4

Case Study – 1

13. In the picture given below, one can see a rectangular in-ground swimming pool installed by a family in their backyard. There is a concrete sidewalk around the pool of width x m. The outside edges of the sidewalk measure 7 m and 12 m. The area of the pool is 36 sq. m.



- (a) Based on the information given above, form a quadratic equation in terms of x .
- (b) Find the width of the sidewalk around the pool.

2

2



Case Study – 2

14. John planned a birthday party for his younger sister with his friends. They decided to make some birthday caps by themselves and to buy a cake from a bakery shop. For these two items, they decided the following dimensions :

Cake : Cylindrical shape with diameter 24 cm and height 14 cm.

Cap : Conical shape with base circumference 44 cm and height 24 cm.



Based on the above information, answer the following questions :

- (a) How many square cm paper would be used to make 4 such caps ? 2
- (b) The bakery shop sells cakes by weight (0.5 kg, 1 kg, 1.5 kg, etc.). To have the required dimensions, how much cake should they order, if 650 cm^3 equals 100 g of cake ? 2