

Series : GE1FH



SET~3

रोल नं.
Roll No.



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नोट

- (I) कृपया जाँच कर लें कि इस प्रश्न-पत्र में मुद्रित पृष्ठ **27** हैं।
- (II) प्रश्न-पत्र में दाहिने हाथ की ओर दिए गए प्रश्न-पत्र कोड को परीक्षार्थी उत्तर-पुस्तिका के मुख-पृष्ठ पर लिखें।
- (III) कृपया जाँच कर लें कि इस प्रश्न-पत्र में **38** प्रश्न हैं।
- (IV) कृपया प्रश्न का उत्तर लिखना शुरू करने से पहले, उत्तर-पुस्तिका में यथा स्थान पर प्रश्न का क्रमांक अवश्य लिखें।
- (V) इस प्रश्न-पत्र को पढ़ने के लिए 15 मिनट का समय दिया गया है। प्रश्न-पत्र का वितरण पूर्वाह्न में 10.15 बजे किया जाएगा। 10.15 बजे से 10.30 बजे तक परीक्षार्थी केवल प्रश्न-पत्र को पढ़ेंगे और इस अवधि के दौरान वे उत्तर-पुस्तिका पर कोई उत्तर नहीं लिखेंगे।

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प्रश्न-पत्र कोड

Q.P. Code

430/1/3

परीक्षार्थी प्रश्न-पत्र कोड को उत्तर-पुस्तिका के मुख-पृष्ठ पर अवश्य लिखें।

Candidates must write the Q.P. Code on the title page of the answer-book.

NOTE

- (I) Please check that this question paper contains **27** printed pages.
- (II) Q.P. Code given on the right hand side of the question paper should be written on the title page of the answer-book by the candidate.
- (III) Please check that this question paper contains **38** questions.
- (IV) **Please write down the Serial Number of the question in the answer-book at the given place before attempting it.**
- (V) 15 minute time has been allotted to read this question paper. The question paper will be distributed at 10.15 a.m. From 10.15 a.m. to 10.30 a.m., the candidates will read the question paper only and will not write any answer on the answer-book during this period.



गणित (बुनियादी)

MATHEMATICS (BASIC)

निर्धारित समय : **3 घण्टे**

Time allowed : 3 hours

अधिकतम अंक : **80**

Maximum Marks : 80



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General Instructions :

Read the following instructions very carefully and strictly follow them :

- (i) *This question paper contains **38** questions. **All** questions are **compulsory**.*
- (ii) *This question paper is divided into **five** Sections – **A, B, C, D** and **E**.*
- (iii) *In **Section A**, Questions no. **1** to **18** are Multiple Choice Questions (MCQs) and questions number **19** and **20** are Assertion-Reason based questions of **1** mark each.*
- (iv) *In **Section B**, Questions no. **21** to **25** are Very Short Answer (VSA) type questions, carrying **2** marks each.*
- (v) *In **Section C**, Questions no. **26** to **31** are Short Answer (SA) type questions, carrying **3** marks each.*
- (vi) *In **Section D**, Questions no. **32** to **35** are Long Answer (LA) type questions carrying **5** marks each.*
- (vii) *In **Section E**, Questions no. **36** to **38** are case study based questions carrying **4** marks each. Internal choice is provided in **2** marks questions in each case study.*
- (viii) *There is no overall choice. However, an internal choice has been provided in 2 questions in Section B, 2 questions in Section C, 2 questions in Section D and 3 questions in Section E.*
- (ix) *Draw neat diagrams wherever required. Take $\pi = \frac{22}{7}$ wherever required, if not stated.*
- (x) *Use of calculator is **not** allowed.*

SECTION A

*This section has **20** Multiple Choice Questions (MCQs) carrying **1** mark each. $20 \times 1 = 20$*

- 1. The ratio of the area of a quadrant of a circle to the area of the same circle is :
 - (A) 1 : 2
 - (B) 2 : 1
 - (C) 1 : 4
 - (D) 4 : 1
- 2. For which of the following solids is the lateral/curved surface area and total surface area the same ?
 - (A) Cube
 - (B) Cuboid
 - (C) Hemisphere
 - (D) Sphere



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3. The class mark of the median class of the following data is :

<i>Class Interval</i>	10 – 25	25 – 40	40 – 55	55 – 70	70 – 85	85 – 100
<i>Frequency</i>	2	3	7	6	6	6

- (A) 40
(B) 55
(C) 47.5
(D) 62.5
4. The following distribution shows the number of runs scored by some batsmen in test matches :

<i>Runs Scored</i>	3000 – 4000	4000 – 5000	5000 – 6000	6000 – 7000
<i>Number of Batsmen</i>	5	10	9	8

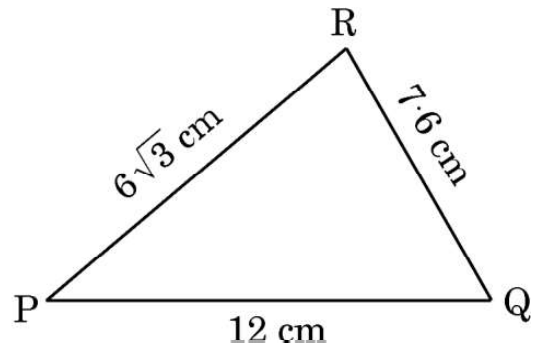
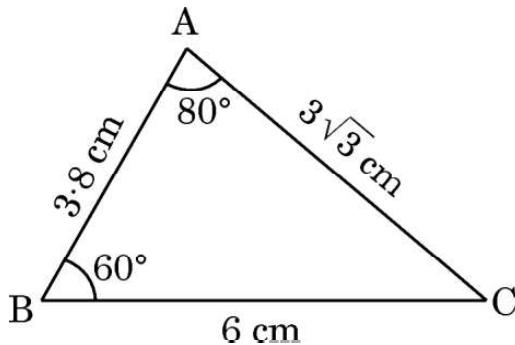
The lower limit of the modal class is :

- (A) 3000
(B) 4000
(C) 5000
(D) 6000
5. In an experiment of throwing a pair of dice, the probability of not getting a doublet is :
- (A) $\frac{1}{6}$ (B) $\frac{5}{6}$
(C) $\frac{1}{5}$ (D) $\frac{1}{30}$
6. If the HCF of two positive integers a and b is 1, then their LCM is :
- (A) a + b (B) a
(C) b (D) ab
7. $(2 + \sqrt{2})^2$ is :
- (A) a rational number (B) an irrational number
(C) an integer (D) a natural number



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8. The discriminant of the quadratic equation $2x^2 - 3x - 5 = 0$ is :
(A) -31 (B) 49
(C) 7 (D) $\sqrt{-31}$
9. The equation $x + \frac{1}{x} = 3$ ($x \neq 0$) is expressed as a quadratic equation in the form of $ax^2 + bx + c = 0$. The value of $a - b + c$ is :
(A) 5 (B) 2
(C) 1 (D) -1
10. For a point $X(a, b)$ where ($b > a > 0$), the value of its [distance from x-axis – distance from y-axis] is :
(A) $a - b$ (B) $b - a$
(C) $a^2 - b^2$ (D) $b^2 - a^2$
11. The mid-point of a line segment divides the line segment in the ratio :
(A) $1 : 2$ (B) $2 : 1$
(C) $1 : 1$ (D) $\frac{1}{2} : 2$
12. Which of the following is **not** the criterion for similarity of triangles ?
(A) AAA (B) SSS
(C) SAS (D) RHS
13. From the figures given below, which of the following is true about the measure of $\angle P$?

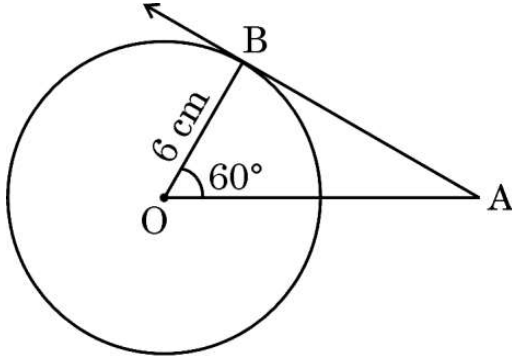


- (A) $\angle P = 60^\circ$
(B) $\angle P = 80^\circ$
(C) $\angle P = 40^\circ$
(D) The measure of $\angle P$ cannot be determined



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14. दी गई आकृति में, यदि AB एक स्पर्श-रेखा O केन्द्र वाले वृत्त पर इस प्रकार बनी है कि $OB = 6 \text{ cm}$ तथा $\angle AOB = 60^\circ$ है, तो OA की लंबाई है :



- (A) 3 cm (B) $3\sqrt{3} \text{ cm}$
(C) $4\sqrt{3} \text{ cm}$ (D) 12 cm

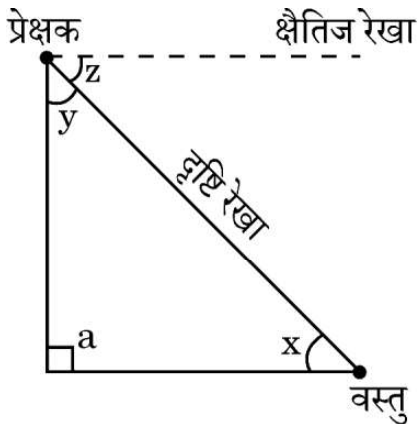
15. निम्नलिखित में से कौन-सा कथन असत्य है ?

- (A) $\tan 45^\circ = \cot 45^\circ$
(B) $\sin 90^\circ = \tan 45^\circ$
(C) $\sin 30^\circ = \cos 30^\circ$
(D) $\sin 45^\circ = \cos 45^\circ$

16. $\left(\frac{1}{\sec^2 A} + \frac{1}{\operatorname{cosec}^2 A} \right)$ का मान है :

- (A) 1 से अधिक (B) 1
(C) 0 (D) -1

17. दी गई आकृति में, निम्नलिखित में से कौन-सा कोण अवनमन कोण है ?

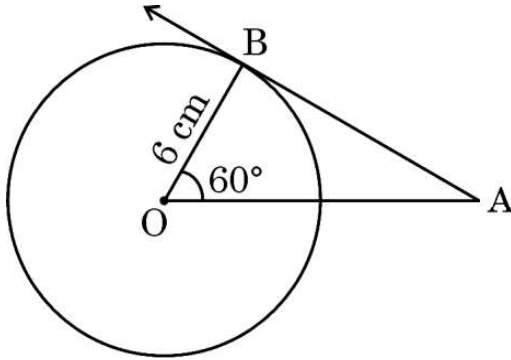


- (A) x
(B) y
(C) z
(D) a

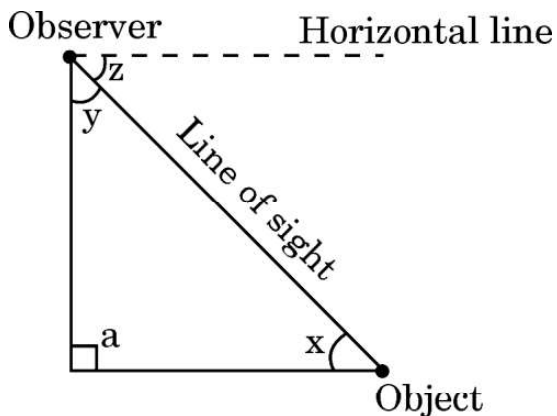


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14. In the given figure, if AB is a tangent to the circle with centre O such that $OB = 6$ cm and $\angle AOB = 60^\circ$, then the length of OA is :



- (A) 3 cm (B) $3\sqrt{3}$ cm
(C) $4\sqrt{3}$ cm (D) 12 cm
15. Which of the following statements is **false** ?
(A) $\tan 45^\circ = \cot 45^\circ$
(B) $\sin 90^\circ = \tan 45^\circ$
(C) $\sin 30^\circ = \cos 30^\circ$
(D) $\sin 45^\circ = \cos 45^\circ$
16. The value of $\left(\frac{1}{\sec^2 A} + \frac{1}{\operatorname{cosec}^2 A} \right)$ is :
(A) more than 1 (B) 1
(C) 0 (D) -1
17. In the given figure, which of the following angles represents the angle of depression ?

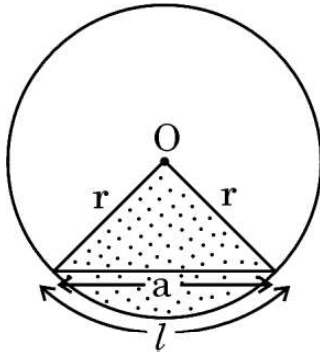


- (A) x
(B) y
(C) z
(D) a



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18. The perimeter of the shaded region in the given figure is :



- (A) l
 (B) $l + a$
 (C) $l + 2r$
 (D) $l + 2r + a$

Questions number 19 and 20 are Assertion and Reason based questions. Two statements are given, one labelled as Assertion (A) and the other is labelled as Reason (R). Select the correct answer to these questions from the codes (A), (B), (C) and (D) as given below.

- (A) Both Assertion (A) and Reason (R) are true and Reason (R) is the correct explanation of Assertion (A).
 (B) Both Assertion (A) and Reason (R) are true, but Reason (R) is **not** the correct explanation of Assertion (A).
 (C) Assertion (A) is true, but Reason (R) is false.
 (D) Assertion (A) is false, but Reason (R) is true.

19. Assertion (A) : For any two natural numbers a and b, the HCF of a and b is a factor of the LCM of a and b.

Reason (R) : HCF of any two natural numbers divides both the numbers.

20. Assertion (A) : The value of p for which the system of equations $4x + py + 8 = 0$ and $2x + 2y + 2 = 0$ is consistent is 4.

Reason (R) : The system of equations $a_1x + b_1y = c_1$ and $a_2x + b_2y = c_2$ is consistent with infinitely many solutions, if $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$.



खण्ड ख

इस खण्ड में 5 अति लघु-उत्तरीय (VSA) प्रकार के प्रश्न हैं, जिनमें प्रत्येक के 2 अंक हैं।

5×2=10

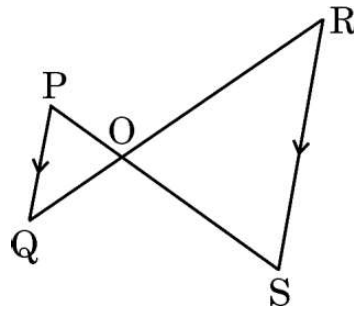
21. 70 cm त्रिज्या की एक वृत्ताकार चादर से एक चतुर्थांश काटा जाता है। बची हुई चादर का क्षेत्रफल ज्ञात कीजिए।

22. x और y के लिए हल कीजिए :

$$3x + 5y = 8$$

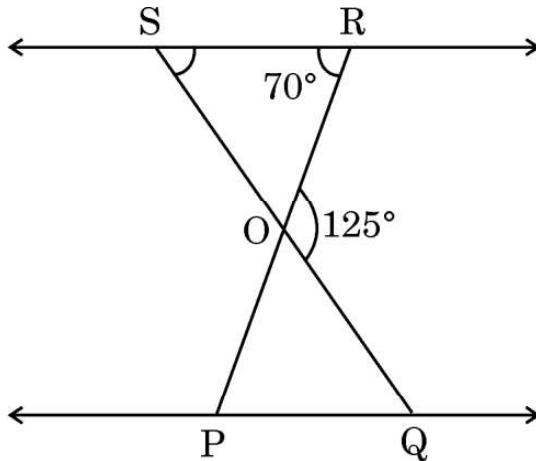
$$5x - 3y = 2$$

23. (क) दी गई आकृति में, यदि $PQ \parallel RS$ है, तो सिद्ध कीजिए कि $\triangle POQ \sim \triangle SOR$.



अथवा

(ख) दी गई आकृति में, $\triangle OSR \sim \triangle OQP$, $\angle ROQ = 125^\circ$ तथा $\angle ORS = 70^\circ$. $\angle OSR$ और $\angle OQP$ के माप ज्ञात कीजिए।



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SECTION B

This section has 5 Very Short Answer (VSA) type questions carrying 2 marks each. $5 \times 2 = 10$

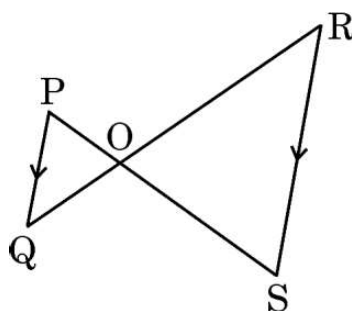
21. From a circular sheet of radius 70 cm, a quadrant is cut. Find the area of the remaining sheet.

22. Solve for x and y :

$$3x + 5y = 8$$

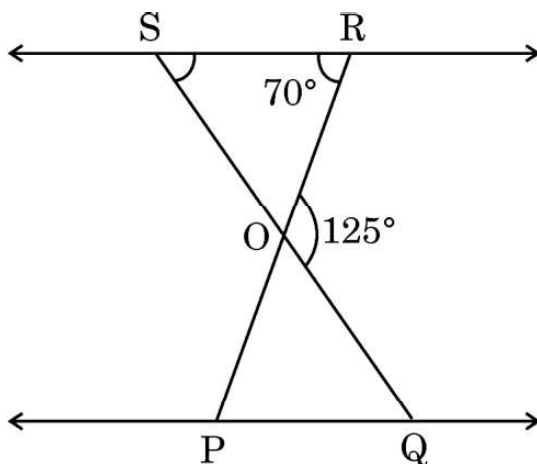
$$5x - 3y = 2$$

23. (a) In the given figure, if $PQ \parallel RS$, then prove that $\triangle POQ \sim \triangle SOR$.



OR

(b) In the given figure, $\triangle OSR \sim \triangle OQP$, $\angle ROQ = 125^\circ$ and $\angle ORS = 70^\circ$. Find the measures of $\angle OSR$ and $\angle OQP$.



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24. Two concentric circles are of radii 6 cm and 10 cm. Find the length of the chord of the larger circle which touches the smaller circle.
25. (a) Find the values of A and B ($0 \leq A < 90^\circ$, $0 \leq B < 90^\circ$), if $\tan(A + B) = 1$ and $\tan(A - B) = \frac{1}{\sqrt{3}}$.

OR

- (b) Prove that $\tan 45^\circ = 1$ geometrically.

SECTION C

This section has 6 Short Answer (SA) type questions carrying 3 marks each. $6 \times 3 = 18$

26. Prove the following trigonometric identity :

$$(\sin A - \operatorname{cosec} A)(\cos A - \sec A) = \frac{1}{\tan A + \cot A}$$

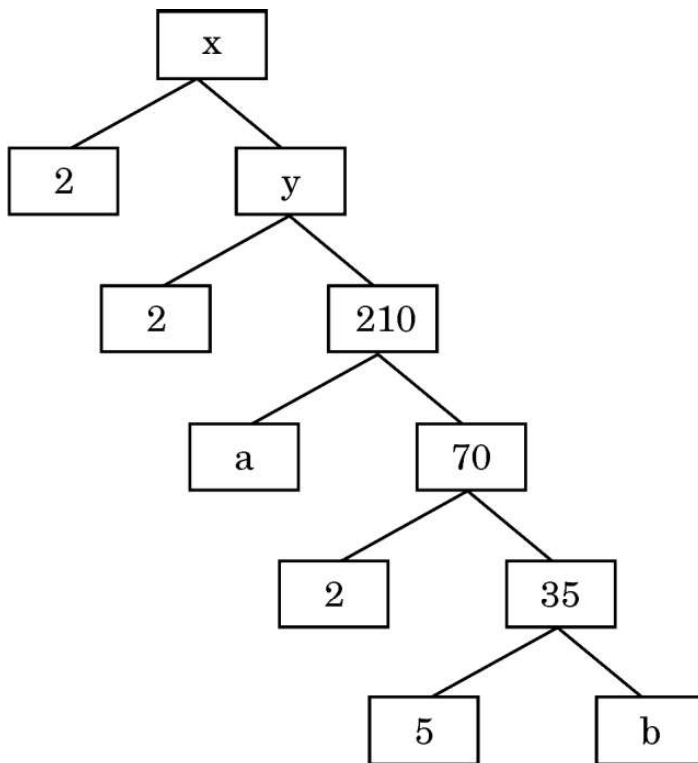
27. A lot consists of 200 pens of which 180 are good and the rest are defective. A customer will buy a pen if it is not defective. The shopkeeper draws a pen at random and gives it to the customer. What is the probability that the customer will not buy it ? Another lot of 100 pens containing 80 good pens is mixed with the previous lot of 200 pens. The shopkeeper now draws one pen at random from the entire lot and gives it to the customer. What is the probability that the customer will buy the pen ?
28. (a) Prove that $\sqrt{3}$ is an irrational number.

OR



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- (b) The factor tree of a number x is shown below :



Find the values of x , y , a and b . Hence, write the product of the prime factors of the number x so obtained.

29. Determine a quadratic polynomial, sum and product of whose zeroes are -10 and 24 , respectively. Also, determine the zeroes of the polynomial so obtained.

30. (a) Solve the following system of equations graphically :

$$x + 3y = 6; \quad 2x - 3y = 12$$

OR

- (b) x and y are complementary angles such that $x : y = 1 : 2$. Express the given information as a system of linear equations in two variables and hence solve it.

31. Prove that a rectangle circumscribing a circle is a square.



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SECTION D

This section has 4 Long Answer (LA) type questions carrying 5 marks each. $4 \times 5 = 20$

- 32.** A life insurance agent found the following data for the distribution of 100 policy holders on the basis of their ages.

<i>Age (in years)</i>	<i>Number of policy holders</i>
15 – 20	2
20 – 25	4
25 – 30	18
30 – 35	21
35 – 40	33
40 – 45	11
45 – 50	3
50 – 55	6
55 – 60	2

Find the median age of the policy holders.

- 33.** (a) The difference of the squares of two positive numbers is 180. The square of the smaller number is 8 times the greater number. Find the two numbers.

OR

- (b) Find the value(s) of k for which the equation $2x^2 + kx + 3 = 0$ has real and equal roots. Hence, find the roots of the equations so obtained.

- 34.** State the converse of “Basic Proportionality Theorem” and use it to prove the following :

Line segment joining mid-points of any two sides of a triangle is parallel to the third side.



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35. (a) A toy is in the form of a cone surmounted on a hemisphere. The cone and hemisphere have the same radii. The height of the conical part of the toy is equal to the diameter of its base. If the radius of the conical part is 5 cm, find the volume of the toy.

OR

- (b) A cubical block is surmounted by a hemisphere of radius 3.5 cm. What is the smallest possible length of the edge of the cube so that the hemisphere can totally lie on the cube ? Find the total surface area of the solid so formed.

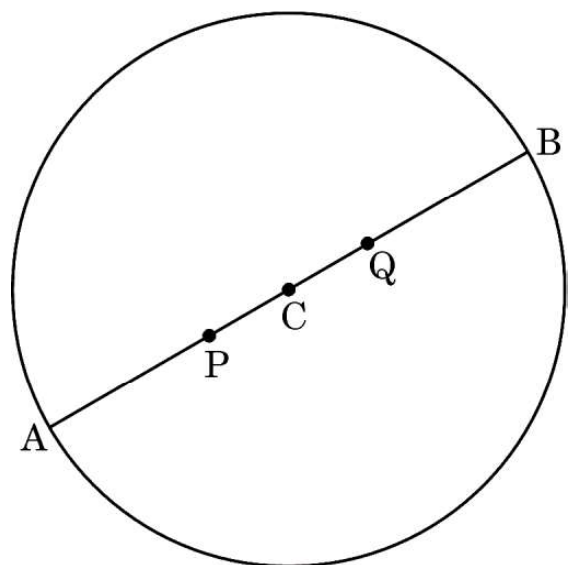
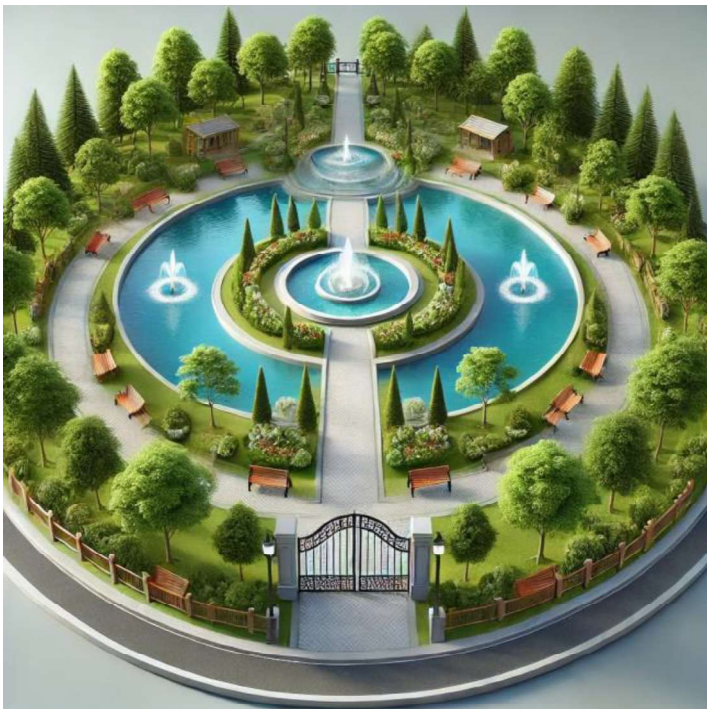
SECTION E

This section has 3 case study based questions carrying 4 marks each.

$3 \times 4 = 12$

Case Study – 1

36. In a society, there is a circular park having two gates. The gates are placed at points A(10, 20) and B(50, 50), as shown in the figure below. Two fountains are installed at points P and Q on AB such that $AP = PQ = QB$.



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Based on the above information, answer the following questions :

- (i) Find the coordinates of the centre C. 1
 - (ii) Find the radius of the circular park. 1
 - (iii) (a) Find the coordinates of the point P. 2
- OR**
- (b) Find the distance of the fountain at Q from gate A. 2

Case Study – 2

37. An injured bird was found on the roof of a building. The building is 15 m high. A fireman was called to rescue the bird. The fireman used an adjustable ladder to reach the roof. He placed the ladder in such a way that the ladder makes an angle of 60° with the ground in order to reach the roof.



Based on the above information, answer the following questions :

- (i) Find the length of the ladder used by the fireman to reach the roof. 1
- (ii) Find the distance of the point on the ground at which the ladder was fixed from the bottom of the building. 1



(iii) In order to avoid skidding, the fireman placed the ladder in such a way that the bottom of the ladder touches the base of the wall which is opposite to the building, making an angle of 30° with the ground.

- (a) Draw a neat diagram to represent the above situation and hence find the width of the road between the building and the wall.

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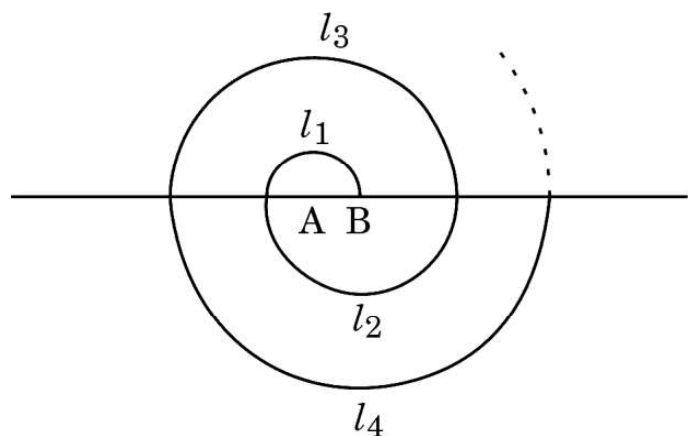
OR

- (b) Find the length of the ladder used by the fireman in this case.

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Case Study – 3

38. In a garden, saplings of rose flowers were planted at equal intervals to form a spiral pattern. The spiral is made up of successive semicircles, with centres alternatively at A and B, starting with centre at A, of radii 50 cm, 100 cm, 150 cm, as shown in the figure given below. Spiral 1 has 10 flowers, Spiral 2 has 20 flowers, Spiral 3 has 30 flowers and so on.



Based on the above information, answer the following questions :

- (i) What is the radius of the 13th spiral ?

1



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(ii) यदि n वीं सर्पिल की त्रिज्या 500 cm है, तो n का मान ज्ञात कीजिए। 1

(iii) (क) 11वीं सर्पिल तक कुल कितने पौधे लगाए गए? 2

अथवा

(ख) कौन-सी सर्पिल तक, कुल 450 पौधे लगे होंगे? 2



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(ii) If the radius of the n^{th} spiral is 500 cm, find the value of n . 1

(iii) (a) Find the total number of saplings till the 11^{th} spiral. 2

OR

(b) Till which spiral, will there be a total of 450 saplings ? 2

